Strategic Games

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Outline

- Today: non-cooperative games
 - ${\scriptscriptstyle \odot}$ A central topic in Game theory: Strategic Games and Nash
 - Additional topics to provide a broader view of the field.
- Tomorrow: cooperative games

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We can abstract this game and provide a generic game representation as follows:

Definition (Normal form game)

A normal form game (NFG) is $(N,(S_i)_{i\in N},(u)_{i\in N})$ where

- N is the set of n players.
- \circ S_i is the set of strategies available to agent i.
- $u_i: S_1 \times \cdots \times S_n \to \mathbb{R}^n$ is the payoff function of agent i. It maps a strategy profile to a utility.

Terminology:

- an element $s = \langle s_1, ..., s_n \rangle$ of $S_1 \times \cdots \times S_n$ is called a strategy profile or a joint-strategy.
- \circ Let $s \in S_1 \times \cdots \times S_n$ and $s_i' \in S_{i^*}$ We write (s_i', s_{-i}) the joint-strategy which is the same as s except for agent i which plays strategy s_i' , i.e., $(s_i', s_{-i}) = \langle s_1, \dots, s_{i-1}, s_i', s_{i+1}, \dots, s_n \rangle$

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Definition (strong dominance)

A strategy $x \in S_i$ for player i (strongly) dominates another strategy $y \in S_i$ if independently of the strategy played by the opponents, agent *i* (strictly) prefers *x* to *y*, i.e. $\forall s \in$ $S_1 \times \cdots \times S_n$, $u_i(x, s_{-i}) > u_i(y, s_{-i})$

well.

Prisoner's dilemma

Both players have a dominant strategy: to confess! From Row's point of view:

	C confesses	C does not
R confesses	2,2	4,1
R does not	1,4	3,3

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- o if C confesses: R is better off confessing as
- o if C does not: R can exploit and confess.

Prisoner's dilemma

Agents have goals, they want to bring about some states of

the world, they can take actions in their environment. o In a multiagent system, agents interact, the actions of one

• How can we formally model such interactions? • How should rational agents behave? Game theory is one way.

may affect many other agents.

Two partners in crime, Row (\mathbb{R}) and Column (\mathbb{C}), are arrested by the police and are being interrogated in separate rooms. From Row's point of view, four different outcomes can occur:

- Only R confesses →R gets 1 year.
- $\,\circ\,$ Only C confesses $\,eole\,R$ spends 4 years in jail.
- Both confess -Both spend 3 years in prison.
- Neither one confesses

 both get 2 years in prison.

The utility of an agent is (5 - number of years in prison).

	Column confesses	Column does not
Row confesses	2,2	4,1
Row does not	1,4	3,3

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What would you do?

- $N = \{Row, Column\}$
- $\quad \circ \ \, S_{Row} = S_{Column} = \{cooperate, \ defect\}$
- \circ u_{Row} and u_{Column} are defined by the following bi-matrix.

Row \ Column	defect	cooperate
defect	2,2	4,1
cooperate	1,4	3,3

- 1. Wait to know the other action?
- 2. Not confess?
- 3. Confess?

Can you use some general principles to explain your choice?

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Battle of the sexes

	LS	RO
ТО	2,2	4,3
BS	3,4	1,1

- Problem: Where to go on a date: Soccer or Opera?
- Requirements:
 - have a date!
 - be at your favourite place!

Do players have a dominant strategy?

Definition (Best response)

A strategy s_i of a player i is a best response to a jointstrategy s_{-i} of its opponents iff

 $\forall s_i' \in S_i, \ u_i(s_i, s_{-i}) \geqslant u_i(s_i', s_{-i}).$

Definition (Nash equilibrium)

A joint-strategy $s \in S_1 \times \cdots \times S_n$ is a Nash equilibrium if each s_i is a best response to s_{-i} , that is

 $(\forall i \in N) (\forall s_i' \in S_i) u_i(s_i, s_{-i}) \geqslant u_i(s_i', s_{-i})$

Battle of the sexes possesses two Nash equilibria $\langle O,S \rangle$ and $\langle S,O \rangle$.

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A Nash equilibrium is a joint-strategy in which no player could improve their payoff by unilaterally deviating from their assigned strategy.

Prisoner's dilemma

Unique Nash equilibrium: both players confess!

	C confesses	C does not
R confesses	2,2 2,2	4,1
D door not	1.4	2.2

if R changes unilaterally, R loses!if C changes unilaterally, C loses!

Definition (Pareto optimal outcome)

A joint-strategy s is a Pareto optimal outcome if for no joint-strategy s^\prime

 $\forall i \in N \ u_i(s') \geqslant u_i(s) \ \text{and} \ \exists i \in N u_i(s') > u_i(s)$

A joint-strategy is a Pareto optimal outcome when there is no outcome that is better for all players.

Prisoner's dilemma: Remaining silent is Pareto optimal.

discussion: It would be rational to confess! This seems counter-intuitive, as both players would be better off by keeping silent.

There is a conflict: the **stable** solution (i.e., the Nash equilibrium) is not **efficient**, as the outcome is not Pareto optimal.

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Nash equilibrium 9

Nash equilibrium: a summary

- When there is no dominant strategy, an equilibrium is the next best thing.
- A game may not have a Nash equilibrium.
- If a game possesses a Nash equilibrium, it may not be unique.
- Any combinations of dominant strategies is a Nash equilibrium.
- A Nash equilibrium may not be Pareto optimal.
- Two Nash equilibria may not have the same payoffs

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Nash equilibrium

Given a mixed strategy profile $p=\langle p_1,\ldots,p_n\rangle$, we write (p_i',p_{-i}) the mixed strategy profile which is the same as p except for player i which plays mixed strategy p_i' , i.e., $(p_i',p_{-i})=\langle p_1,\ldots,p_{i-1},p_i',p_{i+1},\ldots,p_n\rangle$.

Definition (Mixed Nash equilibrium)

A **mixed Nash equilibrium** is a mixed strategy profile p such that $E_i(p) \geqslant E_i(p_i',p_i)$ for every player i and every possible mixed strategy p_i' for i.

Battle of the sexes

	L	R
Т	2,2	4,3
В	3,4	1,1

Let us consider that each player plays the mixed strategy $\langle \frac{3}{4}, \frac{1}{4} \rangle$.

None of the players have an incentive to deviate:

$$E_{row}(T) = \frac{3}{4} \cdot 2 + \frac{1}{4} \cdot 4 = \frac{5}{2}$$
 $E_{row}(B) = \frac{3}{4} \cdot 3 + \frac{1}{4} \cdot 1 = \frac{5}{2}$ (players are indifferent)

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Nash equilibrium 13

Computing a Nash equilibrium

 $\begin{tabular}{ll} \textbf{Complexity:} & In general, it is a hard problem. It is a PPAD-complete problem. \end{tabular}$

Daskalakis, Goldberg, Papadimitriou: The complexity of computing a Nash equilibrium, in *Proc. 38th Ann. ACM Symp. Theory of Computing (STOC)*, 2006

There are complexity results and algorithms for different classes of games. We will not treat then in this tutorial.

Y. Shoham & K. Leyton-Brown: **Multiagent Systems**, Cambridge University Press, 2009. (Chapter 4)

Nisan, Roughgarden, Tardos & Vazirani: Algorithmic Game Theory, Cambridge University Press, 2007. (chapters 2, 3)

Chicken game

In Rebel Without a Cause, James Dean's character's, Jim, is challenged to a "Chickie Run" with Buzz, racing stolen cars towards an abyss. The one who first jumps out of the car loses and is deemed a "chicken" (coward).

	Jim drives on	Jim turns
Buzz drives on	-10,-10	5,0
Buzz turns	0,5	1,1

Dominant Strategy? X Nash equilibrium ? X

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Nash equilibrium 10

Definition (Mixed strategy)

A mixed strategy p_i of a player i is a probability distribution over its strategy space S_i .

Assume that there are three strategies: $S_i = \{1,2,3\}$. Player i may decide to play strategy 1 with a probability of $\frac{1}{3}$, strategy 2 with a probability of $\frac{1}{2}$ and strategy 3 with a probability of $\frac{1}{6}$. The mixed strategy is then denoted as $\left\langle \frac{1}{3}, \frac{1}{2}, \frac{1}{6} \right\rangle$.

Given a mixed strategy profile $p=\langle p_1,\ldots,p_n\rangle$, the expected utility for agent i is computed as follows:

$$E_i(p) = \sum_{s \in S_1 \times \dots \times S_n} \left(\left(\prod_{j \in N} p_j(s_j) \right) \times u_i(s) \right)$$

Battle of the sexes

		y	1-y
		L	R
х	Т	2,2	4,3
1-x	В	3,4	1,1

The expected utility for the Row player is: $xy\cdot 2+x(1-y)\cdot 4+(1-x)y\cdot 3+(1-x)(1-y)\cdot 1=-4xy+3x+2y+1$

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Nash equilibrium

Theorem (J. Nash, 195))

Every finite strategic game has got at least one mixed Nash equilibrium.

note: The proofs are non-constructive and use Brouwer's or Kakutani's fixed point theorems.

J.F. Nash. Equilibrium points in n-person games. in Proc. National Academy of Sciences of the United States of America, 36:48-49, 1950.

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Nash equilibrium 14

Other types of solution concepts for NFGs

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Stéphane Airiau (ILLC) - Strategic Games Nash

Safety strategy

With Nash equilibrium, we assumed that the opponents were rational agents. What if the opponents are potentially ${\color{black} \textbf{malicious}}$, i.e., their goal could be to minimize the payoff of the player?

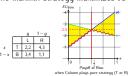
Definition (Maxmin)

For player i,

the maxmin strategy is argmax $\min_{s_i \in S_i} \min_{s_{-i} \in S_{-i}} u_i(s_i, s_{-i})$,

and its maxmin value or safety level is $\max_{s_i \in S_i} \min_{s_i \in S_{-i}} u_i(s_i, s_{-i})$.

- 1) player i chooses a (possibly mixed) strategy. 2) the opponents -i choose a (possible mixed) strategy that $minimize\ i$'s payoff.
- the maxmin strategy maximizes i's worst case payoff.



Whatever Column does, Row can guarantee itself a payoff of 2.5 by playing the mixed strategy $\langle \frac{1}{2}, \frac{1}{2} \rangle$.

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Minimax theorem

Theorem

Minimax theorem (von Neumann, 1928)

In any finite two-player zero-sum game, for each player i, the maxmin strategy and minmax strategies are the same and are a Nash equilibrium of the game.

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Correlated equilibrium

Battle of the sexes

	L	R
Т	2,2	4,3
В	3,4	1,1

How to avoid the bad outcomes in which the agents fail to coordinate?

🔽 idea: using a public random variable.

Example: the night before, the couple may condition their strategies based on weather (in the Netherlands, it is raining with a probability of 50%) as follows:

- if it rains at 5pm, we go to opera, otherwise, we go to football.—both players increase their expected utility
- maybe a fairer solution

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For every Nash equilibrium, there exists a corresponding correlated equilibrium.

Proof

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Let s^{\star} be a Nash equilibrium. We define

- \circ $D_i = S_i$: strategy space and the domains of the random variables are the same.
- $\pi(d) = \prod_{i \in N} s^*(d_i)$
- $\circ \sigma_i: D_i \to S_i, d_i \mapsto s_i.$

 Since a Nash equilibrium always exists, a correlated equilibrium always exists as well.

- However, a correlated equilibrium may not be a Nash equilibrium
- correlated equilibrium is a generalization of Nash equilibrium.

Punish

Definition (Minmax)

For player i in a 2-player game, the minmax strategy is $\underset{s_{-i} \in S_{-i}}{\min} \max_{s_i \in S_i} u_i(s_i, s_{-i})$,

and its minmax value is $\min_{s_{-i} \in S_{-i}} \max_{s_i \in S_i} u_i(s_i, s_{-i})$.

Player i's strategy against player -i in a 2-player game is a strategy that minimizes -i's best-case payoff Proposition

For a player i,

$$\max_{s_i \in S_i} \min_{s_{-i} \in S_{-i}} u_i(s_i, s_{-i}) \leqslant \min_{s_{-i} \in S_{-i}} \max_{s_i \in S_i} u_i(s_i, s_{-i})$$

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Minimax regret

Instead of assuming the opponents are rational (Nash equilibrium) or malicious (minimax), one can assume the opponent is unpredictable avoid costly mistakes/minimize their worst-case losses.

	L	R
Т	100,100	0,0
В	0,0	1,1

(T, L) is preferred by both agents. However, (B,R) is also a NE. There is no dominance. How to explain that (T,L) should be preferred?

One can build a regret-recording game where the payoff function r_i is defined by $r_i(s_i,s_{-i}) = u_i(s_i^*,s_{-i}) - u_i(s_i,s_{-i})$, where s_i^* is i's best response to s_{-i} , i.e., $r_i(s_i,s_{-i})$ is i's regret to have chosen s_i instead of s_i

$r_i \backslash r_j$	L	R
T	0,0	1,100
В	100,1	0,0

We define $regret_i(s_i)$ as the maximal regret ican have from choosing s_i .

A regret minimization strategy is one that minimizes the $regret_i$ function.

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Definition (Correlated equilibrium)

Given an *n*-agent game $G = (N, (S)_{i \in N}, (u_i)_{i \in N})$, a correlated equilibrium is a tuple (v, π, σ) , where

- v is a tuple of random variables $v = \langle v_1, \dots, v_n \rangle$ with respective domains $D = \langle D_1, \dots, D_n \rangle$,
- \circ π is a joint-distribution over v,
- \circ $\sigma = \langle \sigma_1, \ldots, \sigma_n \rangle$ is a vector of mappings $\sigma_i : D_i \to S_i$,
- \bullet and for each agent i and every mapping $\sigma'_i:D_i\to S_i$ it is the case that

$$\begin{array}{l} \sum_{d \in D} \pi(d) u_i(\sigma_1(d_1), \dots, \sigma_i(d_i), \dots, \sigma_n(d_n)) \geqslant \\ \sum_{d \in D} \pi(d) u_i(\sigma_1(d_1), \dots, \sigma_i'(d_i), \dots, \sigma_n(d_n)). \end{array}$$

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- We have considered games where each player choose their action simultaneously, and we have studied the normal-form representation.
- $\,\circ\,$ They are many games which rely on turn-taking, e.g., chess, card games, etc. Game theory has something to say about these games as well.
- We now introduce the extended-form games (EFGs), in which a game is represented using a tree structure

Extended Form Games (EFGs)

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A game is described by a game tree.

- o the leaf nodes contain the payoff to the agents.
- the non-leaf nodes are choice nodes, labeled with the agent that make the decision for the node.
- The game tree is common knowledge before the agents start to play.
- During the play, the agents know which actions have been chosen in the past: this is called the perfect

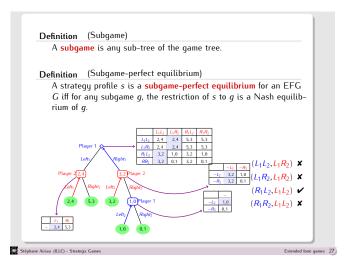
information case.

A strategy is a complete plan of actions of a player: a strategy specifies an action for each of its choice node.

Perfect-information game

ex: Player 1 decides for two nodes and has four strategies: (Left, Left), (Left, Right), (Right, Left) and (Right, Right).

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A congestion game is a tuple $(N,R,(S_i)_{i\in N},(c_r)_{r\in R})$ where:

- $N = \{1, ..., n\}$ is the set of players
- $\circ R = \{1, ..., m\}$ is the set of facilities or **resources**
- $c_r(k)$ is the **cost** related to each user of resource $r \in M$ when exactly \boldsymbol{k} players are using it.

Theorem

Every finite congestion game has a pure strategy Nash equilibrium.

R. W. Rosenthal. A class of games possessing pure-strategy Nash equilibria, in International Journal of Game Theory, 1973.

Theorem

Every congestion game is a potential game and every finite potential game is isomorphic to a congestion game

D. Monderer and L. S. Shapley Potential Games, in Games and economic

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Infinitely repeated games

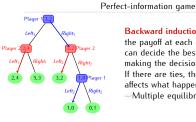
What is a strategy? In a repeated game, a pure strategy depends also on the history of play thus far.

ex: Tit-for-Tat strategy for the prisoner's dilemma: Start by not confessing. Then, play the action played by the opponent during the previous iteration.

What is the players' objective?

- Average criterion: Average payoff received throughout the game by player i: $\lim_{t\to\infty} \frac{\sum_{t=1}^k u_t(s^t)}{t}$, where s^t is the joint-strategy played during iteration t.
- Discounted-sum criterion: Discounted sum of the payoff received throughout the game by player i: $\sum \gamma^t u_i(s^t)$,

where γ is the discount factor (γ models how much the agent cares about the near term compared to long term).



Backward induction: when an agent knows the payoff at each of a node's children, it can decide the best action of the player making the decision for this node. If there are ties, then how they are broken affects what happens higher up in the tree Multiple equilibria...

From an EFG to a NFG

- There can be an exponential number of pure strategies.
- Pure-strategy Nash equilibria of this game are (LL, LR), (LR, LR), (RL, LL), (RR, LL)
- But the only backward induction solution is
- Nash equilibrium may be too weak for EFGs.

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Other models of games

- Congestion games: a special game which always possess a pure strategy Nash equilibrium
- Repeated games: a NFG is played repeatedly (finitely/infinitely many times).
- Stochastic games: uncertainty about the next game to play
- · Bayesian games: uncertainty about the current game

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Repeated games



When players are rational, both players confess!

If they trusted each other, they could both not confess and obtain $\langle 3,3 \rangle$. If the same players have to repeatedly

play the game, then it could be rational not to confess.

- One shot games: there is no tomorrow
- This is the type of games we have studied thus far.
- \circ Repeated games: model a likelihood of playing the game again with the same opponent. The NFG (N,S,u) being repeated is called the stage game.
 - finitely repeated games
 represent using a EFG and use backward induction to solve the game.

 infinitely repeated games: the game tree would be infinite,
 - use different techniques.

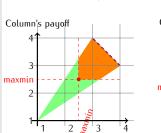
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Theorem (A Folk theorem)

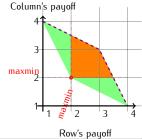
Using the average criterion, any payoff vector v such that

- \circ v is feasible, i.e., $\exists \lambda \in [0,1]^{\prod_{j \in \mathcal{N}} |S_j|}$ s.t. $v_i = \sum_{s \in \prod_{j \in \mathcal{N}} S_j} \lambda_s v_i(s)$
- \circ v is enforceable $v_i \geqslant \max_{s_i \in S_i} \min_{s_{-i} \in S_{-i}} u_i(s_i, s_{-i})$

can be sustained by a Nash equilibrium.



Row's payoff



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Other models of games: repeated games 31

- In repeated games, the same stage game was played repeatedly.
- A Stochastic game is a set of NFGs. The agents repeatedly
 play games from this set. The next game is chosen with a
 probability which depends on the current game and the
 joint-action of the players.

Definition (Stochastic games)

A stochastic game is tuple $(N,(S_i)_{i\in N},Q,P,(u_i)_{i\in N})$ where

- \circ N is the set of players
- \circ S_i is the strategy space of player i
- $\quad \text{$\mathbf{0}$ Q is a set of NFGs $q=(N,(S_i)_{i\in N},(v_i^q)_{i\in N})$}$
- $P: Q \times \prod_{i \in N} S_i \times Q \rightarrow [0,1]$ is the transition function. P(q,s,q') is the probability that game q' is played after game q when the joint-strategy s was played in game q.
- \circ $u_i: Q \times \prod_{i \in N} S_i$ is the payoff function $u_i(q,s)$ is the payoff obtained by agent i when the joint-strategy s was played in game q.

In the definition, for ease of presentation, we assume that all the games have the same strategy space, which is not required.

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Other models of games: stochastic games 33

Evolutionary game theory

- Models organisms in a large population (supposed infinite)
- two organisms are drawn randomly and play a 2-player game.
- the payoffs are linked to the fitness of the agents, and then, to their ability to reproduce.
- when an organism reproduces, a child adopt the same strategy as its parent.
- Goal: Are the strategies used by the organisms resilient to small mutant invasions? I.e, Is a strategy robust to evolutionary pressures?
 - evolutionary stability.

J. W. Weibull, Evolutionary game theory, the MIT press, 1997

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Evolutionary game theory

When does an agent play?

- Agents play simultaneously (Rock/Paper/Scissors) ~NFGs
- Agent play sequentially (chess, card games) ~EFGs

What is known?

- Complete information games: the structure of the game and the preference of the agents are common knowledge.
- Incomplete information games
 - o does a player know the preference of its opponents?
 - uncertainty, learning in games.What kind of opponents? Rational? Malicious?
 - What kind of opponents? Rational? Malicious? Nash equilibrium, minmax, maxmin, regret.

What can be observed? Are the agents able to observe the actions of the opponents (perfect/imperfect information)

How does the game develop?

- Is it a one stage game?
- Are there multiple stages? (repeated games) Does the structure of the game change? —Stochastic, Bayesian games
- Is the game played forever? —Infinitely repeated games

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Conclusions 3

Resources

- Martin J. Osborne and Ariel Rubinstein. A course in Game Theory, the MIT Press, 1994. (freely available online)
- Yoav Shoham and Kevin Leyton-Brown. Multiagent Systems, Cambridge University Press, 2009
- Michael Wooldridge. An Introduction to Multiagent Systems, Wiley, 2009
- Noam Nisan, Tim Roughgarden, Éva Tardos & Vijay V.
 Vazirani. Algorithmic Game Theory, Cambridge University Press, 2007.
- gametheory.net

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- For stochastic games, the players know which game is currently played, i.e., they know the players of the game, the actions available to them, and their payoffs.
- In Bayesian games,
 - there is uncertainty about the game currently being played.
 players have private information about the current game.
 - players have private information about the current game. The definition uses information set.

Definition (Bayesian game)

- A Bayesian game is a tuple $(N, (S_i)_{i \in N}, G, P, (I_i)_{i \in N})$:
 - N is the set of players.
 - S_i is the set of strategies for agent i.
 - G is a set of NFGs $g = (N, (S_i)_{i \in N}, (u_i^g)_{i \in N}).$
 - \circ *P* is a **common prior** over all games in *G*.
 - I_i is the information set of agent i (a partition of G). A player knows the set which includes the current game, she does not know, however, which game it is in the set. ex: G is composed of six games, $I_2 = \{\{g_1, g_3, g_4\}, \{g_2, g_5\}\}$. Agent 2 knows the current game is in $\{g_1, g_3, g_4\}$, but she does not know whether the game is g_1, g_3, g_4 , but she

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Other models of games: bayesian games 34

Summary and Concluding remarks

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Conclusions 3

Nobel	Laureates

1972	Arrow	Social choice
1994	Nash, Selten and Harsanyi	Game theory
1996	Vickrey	Mechanism design
1998	Sen	Social choice
2005	Schelling and Aumann	Game theory
2007	Hurwicz, Maskin and Myerson	Mechanism design

- Game theory: mathematical study of interaction among independent, self-interested agents. (Two sessions at AAMAS-10)
 - non-cooperative games
 - non-cooperative game
 cooperative games
 - games with sequential actions
 - evolutionary game theory
- Mechanism design: study of protocol design for strategic agents (one session at AAMAS-09)
- Social choice: study of preference aggregation / collective decision making. (One session at AAMAS-10)

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Conclusions

Tomorrow

Cooperative games

When agents work together, the group of agents, as a whole, gets a payoff.

- $\, \circ \,$ What groups of agents to form?
- How to distribute the payoff to the individual agents?

39)

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Conclusions