



- From decision theory we borrow the idea of domination among strategies:
- \square x₁ is (obviously) better than x₂ if:

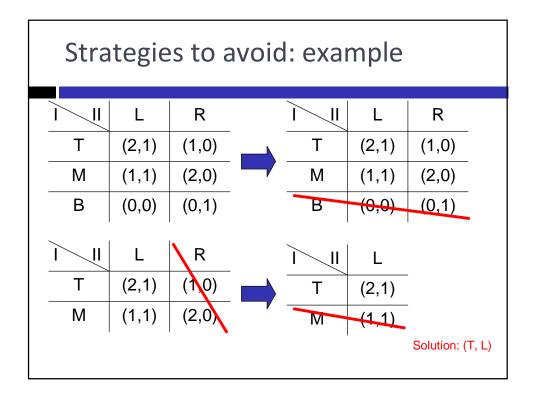
 $h(x_1, y) \supseteq h(x_2, y)$ for every $y \in Y$

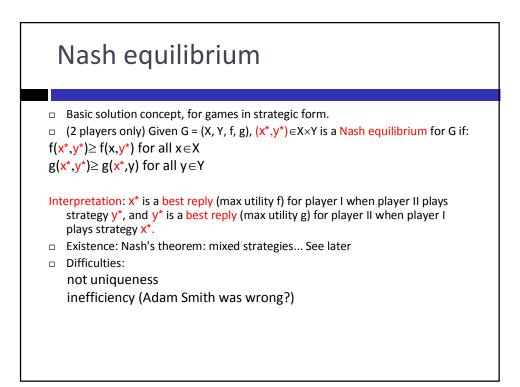
- $\hfill\square$ We shall say that x_1 (strongly) dominates $x_2.$
- $\hfill\square$ So, if x_1 dominates any other $x \in X$, then x_1 is the solution

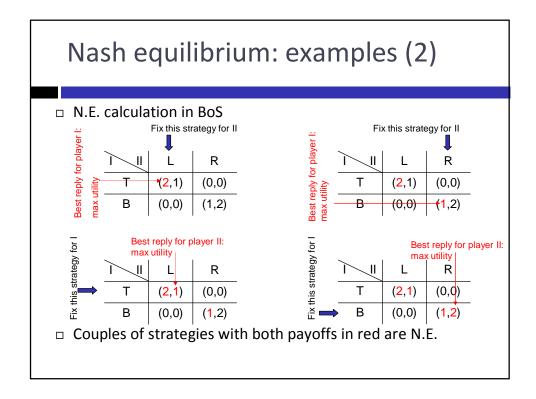
Prisoner's di	lemma						
The game is:		L	R				
	T	(3,3)	(1,4)				
	В	(4,1)	(2,2)				
 Obviously B and R a respectively). So, w easy. 		0	•				
□ But the outcome	But the outcome is inefficient!						
 Both players prefer so? The problem is rational and intellig 	that players		0 ())				

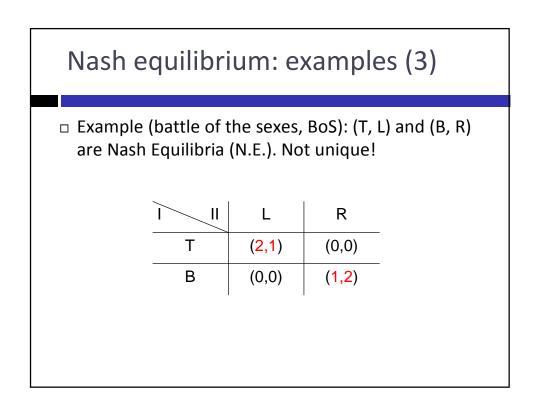


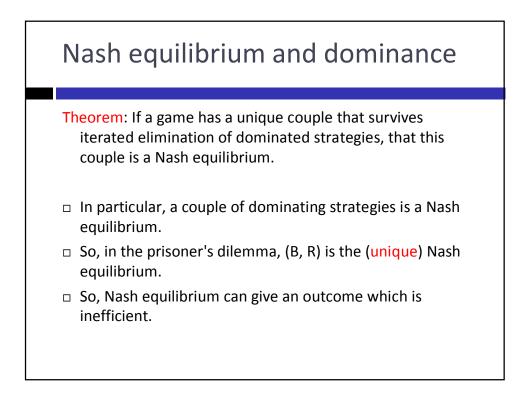
- A strategy which is (strongly) dominated by another one will not be played.
- So we can delete it. But then could appear new (strongly) dominated strategies for the other player. We can delete them.
- $\hfill\square$ And so on...
- □ Maybe players are left with just one strategy each.
- □ Well, a new way to get a solution for the game.
- Technically: solution via iterated elimination of dominated strategies.

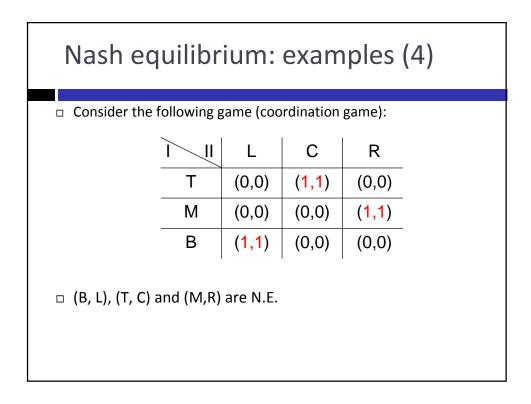


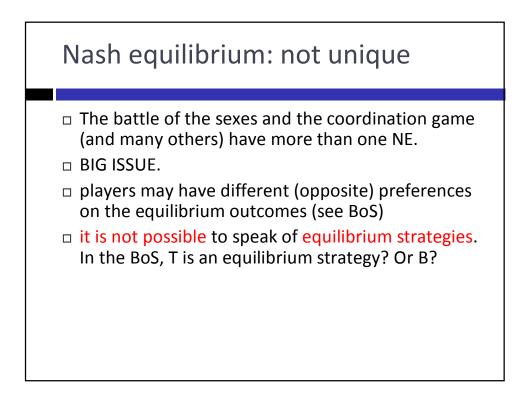












One more problem

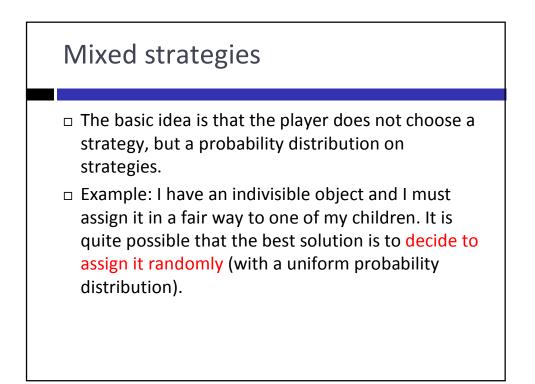
Example: matching pennies (MP)

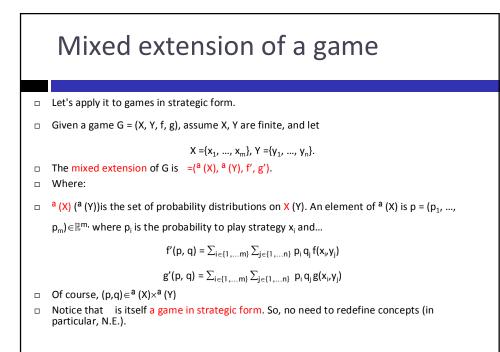
	L	R
Т	(-1, <mark>1</mark>)	(1 ,-1)
В	(1,-1)	(-1, <mark>1</mark>)

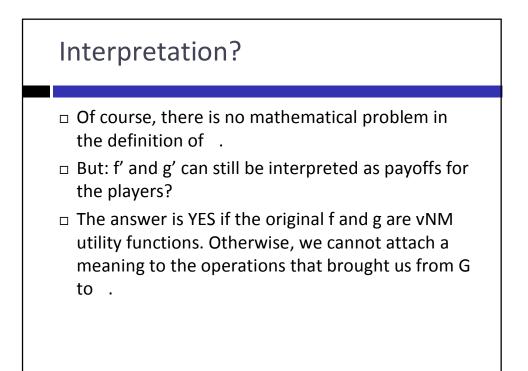
□ There is no equilibrium?

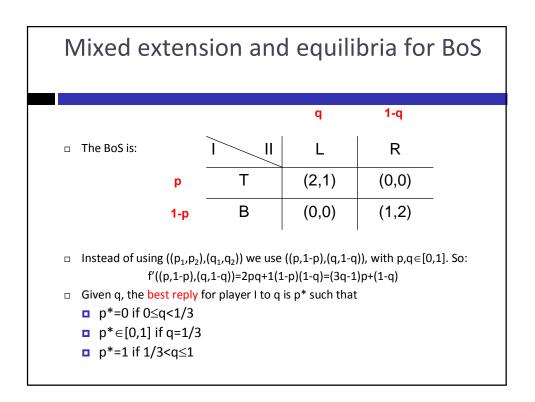
□ But Nash is famous (also) because of his existence thm (1950).

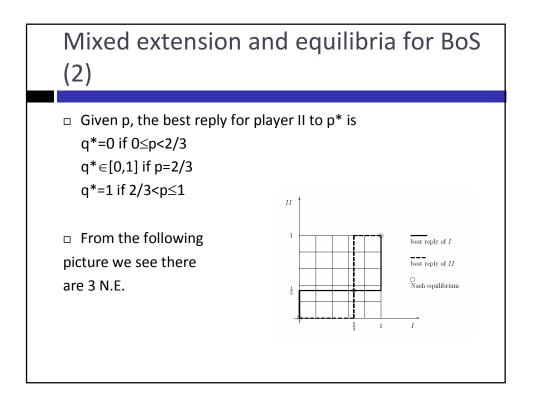
- But MP is a zero-sum game. So, even vN (1928) guarantees that it has an equilibrium.
- $\hfill\square$ Where do we find it? Usual math trick: extend ($\mathbb N$ to $\mathbb Z$, sum to integral, solution to weak solution).

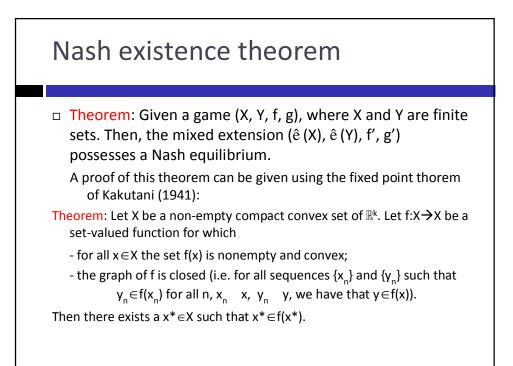


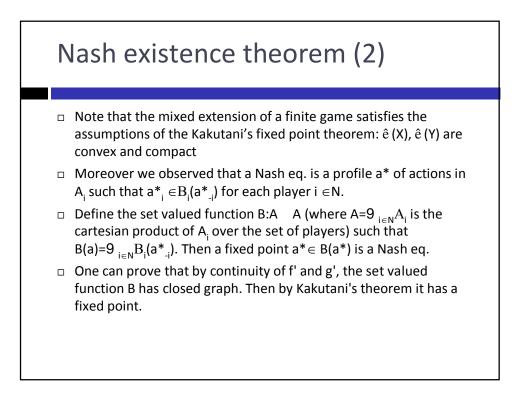


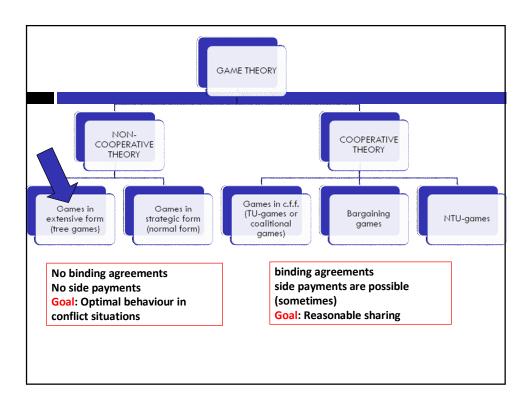


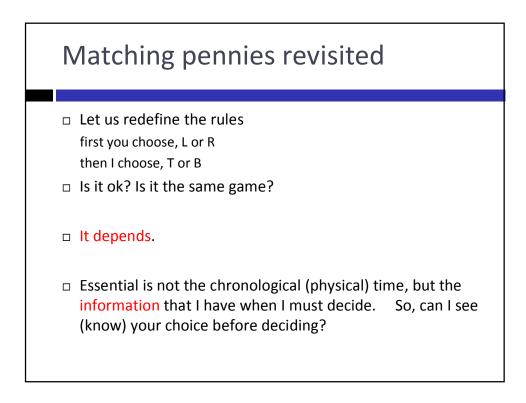


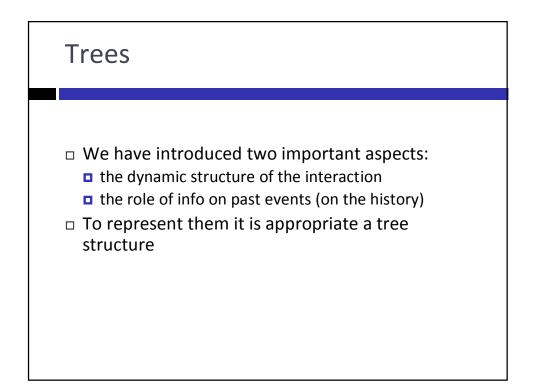


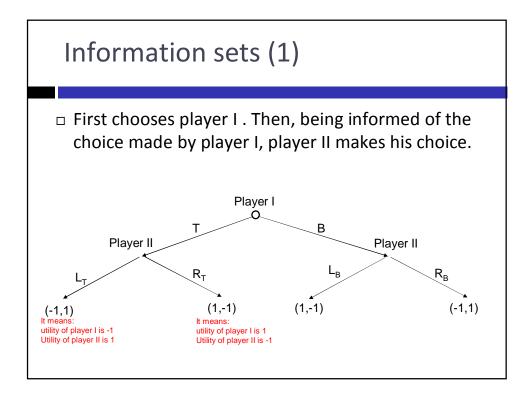


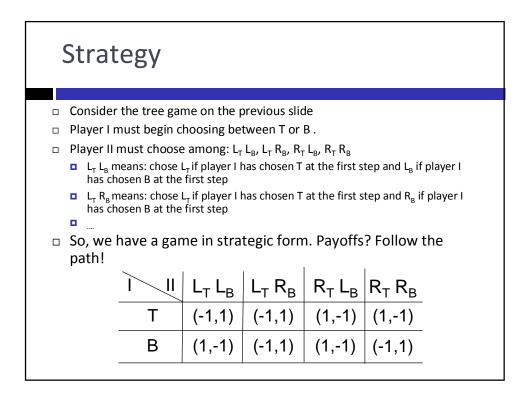


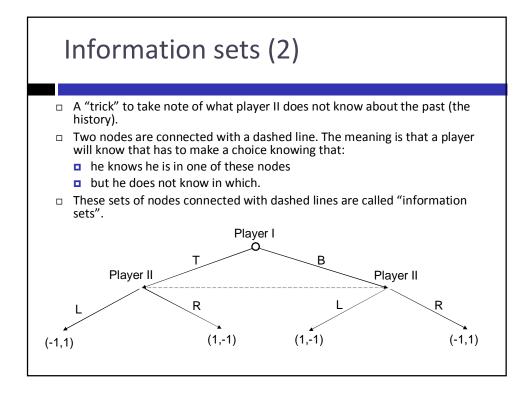


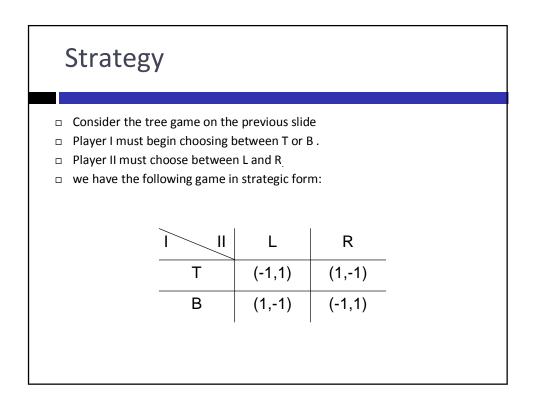


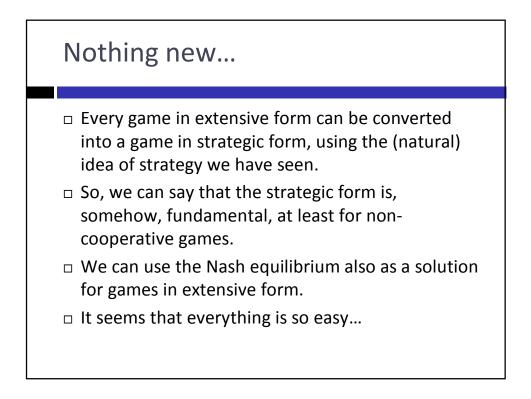






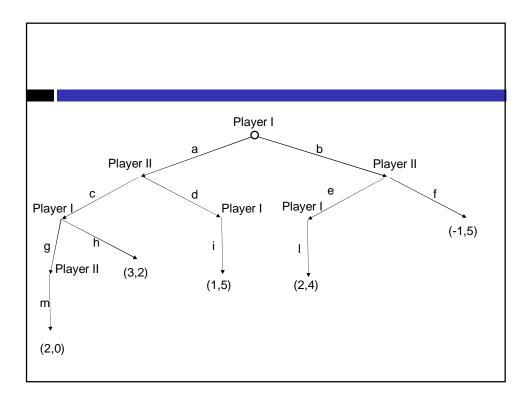


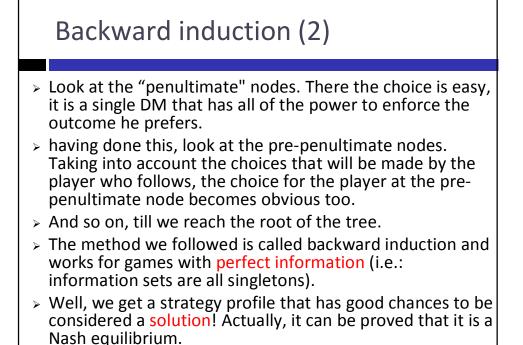


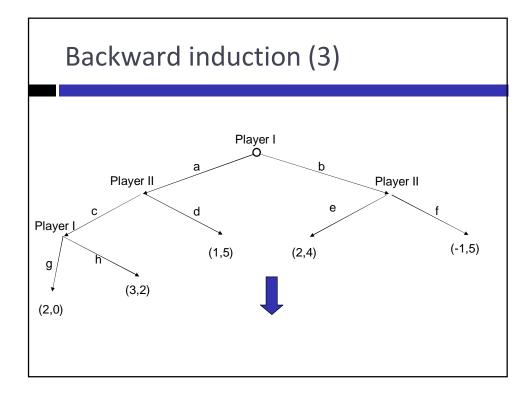


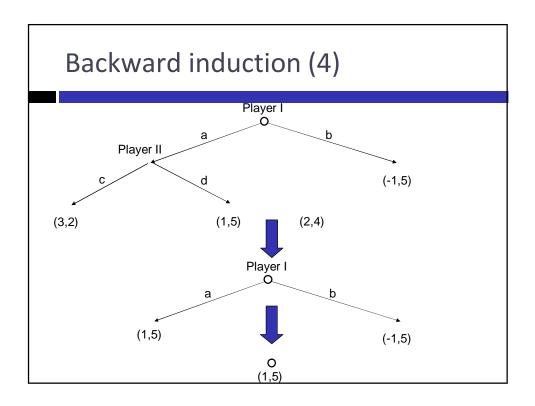
Backward induction

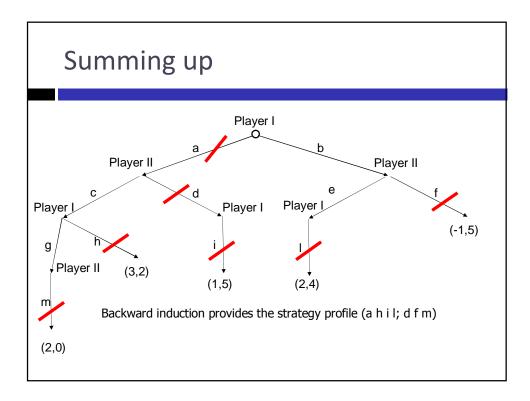
- Consider the very simple game depicted in the following slide
- Player I must begin choosing between a or b. But there is nothing that obliges him to think locally.
- He knows that he could be called to play again. So, before the game starts, he can decide his strategy.
- > It means, choose among: agil, ahil, bgil, bhil.
- > Similarly, II can choose among:cem, cfm, dem, dfm.
- > So, we have a game in strategic form.











Gar	ne in s	strate	egic fo	orm			
			I	I	I		
	Ì	cem	cfm	dem	dfm		
	agil	(2,0)	(2,0)	(1, <mark>5</mark>)	(1 ,5)		
	ahil	(<mark>3</mark> ,2)	(<mark>3</mark> ,2)	(1, <mark>5</mark>)	(1 ,5)		
	bgil	(2,4)	(-1, <mark>5</mark>)	(<mark>2</mark> ,4)	(-1, <mark>5</mark>)		
	bhil	(2,4)	(-1, <mark>5</mark>)	(<mark>2</mark> ,4)	(-1, <mark>5</mark>)		
	(a h i l; d f m) is a Nash equilibrium of the game (actually there is already another Nash equilibrium, but with an equivalent outcome)						

