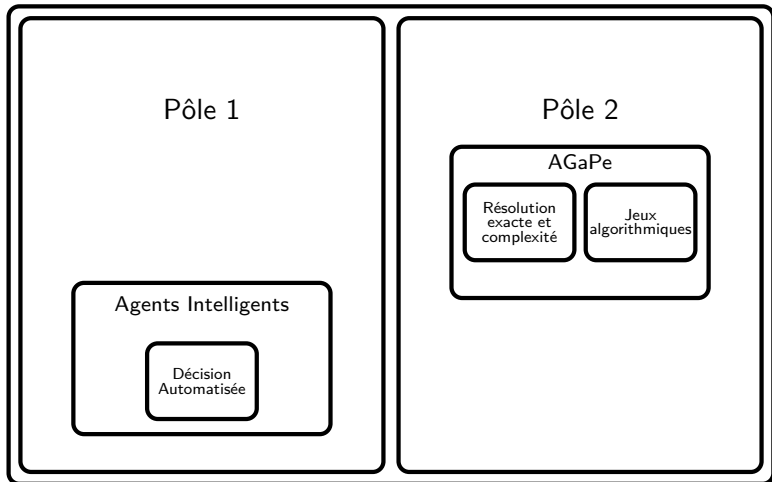


Complexité des jeux de cartes

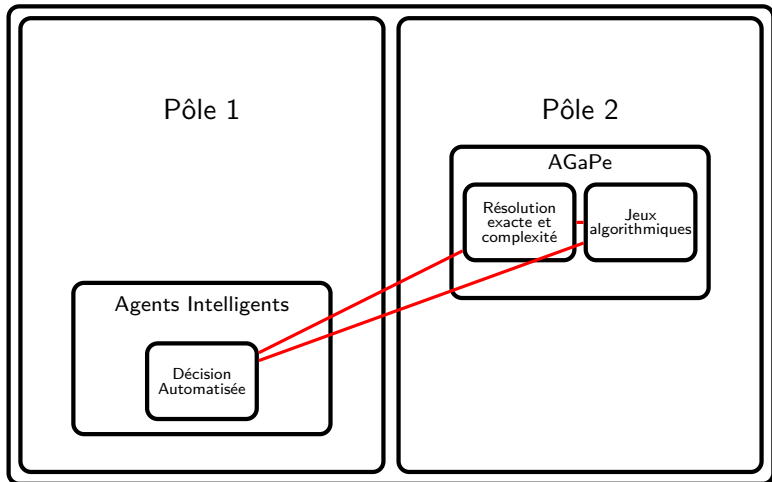
Edouard Bonnet, Florian Jamain, Abdallah Saffidine

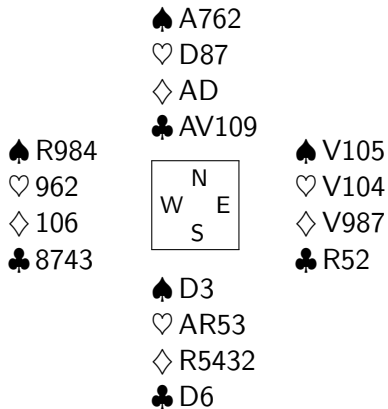
Avril 2013

LAMSADE

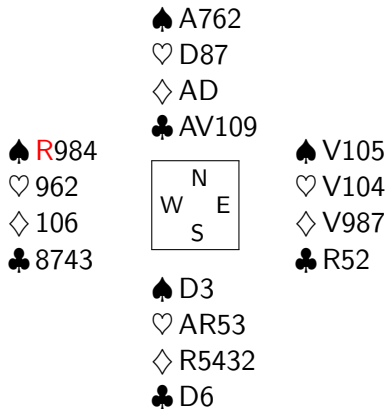


LAMSADE

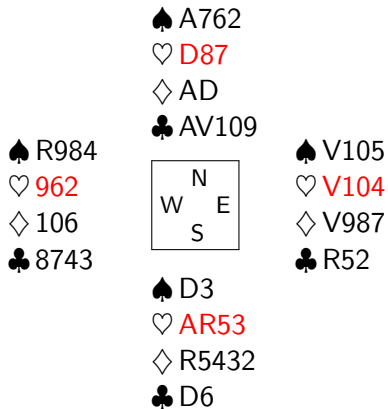




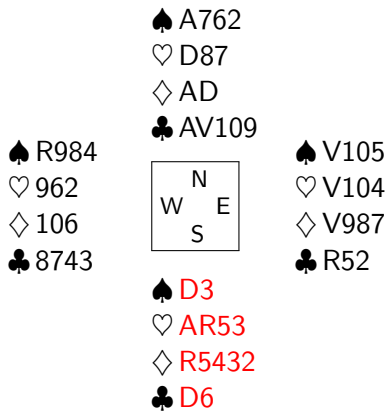
carte, couleur, main, joueur, lancer, fournir, levée.



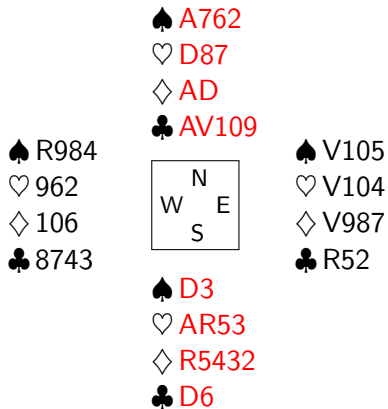
carte, couleur, main, joueur, lancer, fournir, levée.



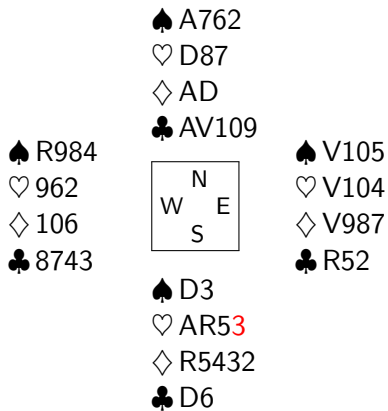
carte, couleur, main, joueur, lancer, fournir, levée.



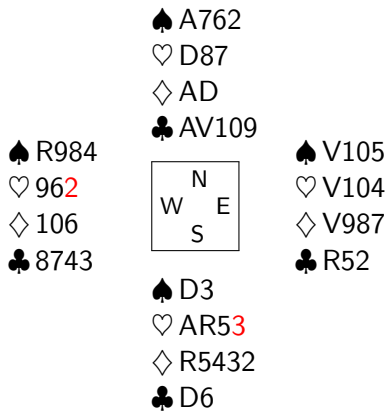
carte, couleur, main, joueur, lancer, fournir, levée.



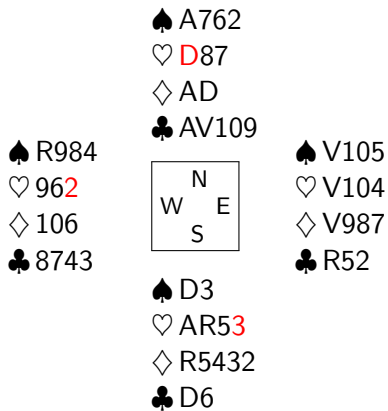
carte, couleur, main, **joueur**, lancer, fournir, levée.



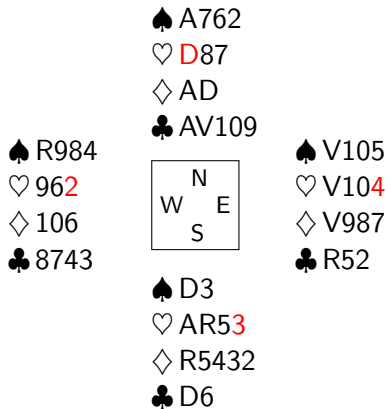
carte, couleur, main, joueur, lancer, fournir, levée.



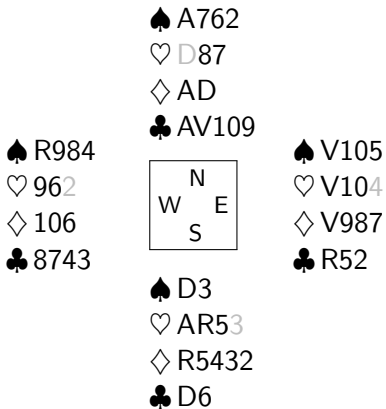
carte, couleur, main, joueur, lancer, **fournir**, levée.



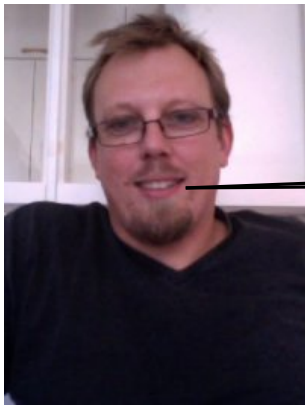
carte, couleur, main, joueur, lancer, **fournir**, levée.



carte, couleur, main, joueur, lancer, **fournir**, levée.



carte, couleur, main, joueur, lancer, fournir, levée.

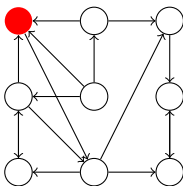


1 main par joueur
et couleurs miroirs
est dans P

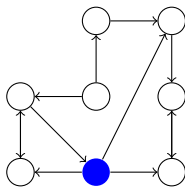


Il n'y a pas de structure géométrique naturelle à exploiter au Bridge

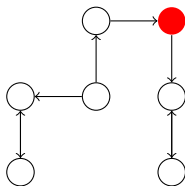
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



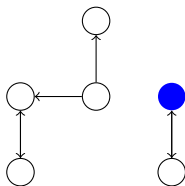
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



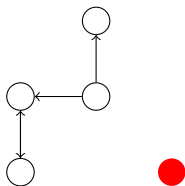
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



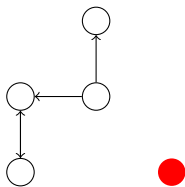
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



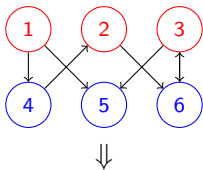
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



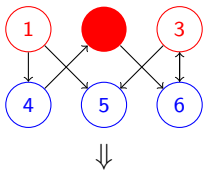
- QBF : $\forall x_1 \exists x_2 \forall x_3 \exists x_4 \dots \forall x_{2n-1} \exists x_{2n} \phi(x_1, \dots, x_{2n})$
- GENERALIZED GEOGRAPHY :



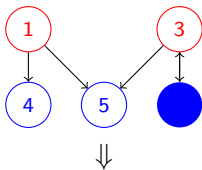
même sur les graphes bipartis



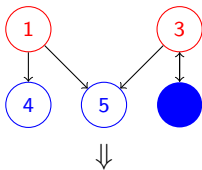
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



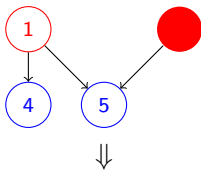
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	c_r	h_r	ARDV109...	c_b	h_b
					ARDV109...



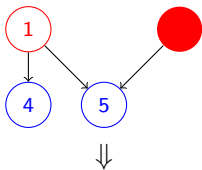
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



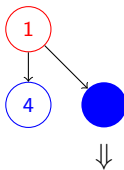
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



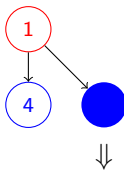
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



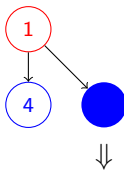
	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		



	h1		h2		h3
c_b	x	c_b	x	c_b	x
$c_{1,4}$	RDV1098...	$c_{2,6}$	RDV1098...	$c_{3,5}$	RDV1098...
$c_{1,5}$	RDV1098...	$c_{4,2}$	A	$c_{3,6}$	RDV1098...
				$c_{6,3}$	A
	h4		h5		h6
c_r	x	c_r	xxx...	c_r	x
$c_{1,4}$	A	$c_{1,5}$	A	$c_{2,6}$	A
$c_{4,2}$	RDV1098...	$c_{3,5}$	A	$c_{3,6}$	A
				$c_{6,3}$	RDV1098...
	h_r		h_b		
c_r	ARDV109...	c_b	ARDV109...		

	h_{r_1}			h_{b_2}	
	c_r	AD108...		c_r	RV97...
	h_{r_2}			h_{b_1}	
c_b	$a_{3W} \dots a_1$	AD108...		c_b	RV97...
		h_r		h_b	
	c_r	x		c_b	x
		⋮			⋮

Si Rouge a W levées d'avance, il gagne en jouant dans c_r .
 Si Bleu a $2W$ levées d'avance, il gagne en jouant dans c_b .

$$c \quad h_r \quad (W+3)(W+2)(W+1)W \dots 321$$

$$c \quad h_b \quad (W+6)(W+5)(W+4)$$

c	h_r	$(W+3)(W+2)(W+1)W\dots 321$	c	h_b	$(W+6)(W+5)(W+4)$
c	h_r	$xxxW$	c	h_b	def
c	h_r	$3 W$	c	h_b	def

h_r

C1		...xx Wx x xW x xW...
C2	...x Wx x xW x xW...	...xx xW x Wx x xW...
C3	...x xW x xW x xW...	...xx xW x xW x Wx...

h_b

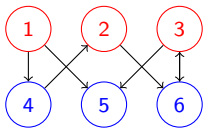
C4	...x Wx x xW x xW...	...xx Wx x xW x xW...
C5	...x Wx x xW x Wx...	...xx xW x Wx x xW...
C6	...x xW x Wx x Wx...	...xx xW x xW x Wx...

h_r

C₁ ...xx Wx x xW x xW...
C₂ ...x Wx x xW x xW... ...xx xW x Wx x xW...
C₃ ...x xW x xW x xW... ...xx xW x xW x Wx...

h_b

C₄ ...x Wx x xW x xW... ...xx Wx x xW x xW...
C₅ ...x Wx x xW x Wx... ...xx xW x Wx x xW...
C₆ ...x xW x Wx x Wx... ...xx xW x xW x Wx...



h_r

c_1					$6 W$	$1 ^{3W/2}$	$\mathcal{A}(c_1)$	$1 ^{3W/2}$
c_2	$4 ^{W/2}$	$3 2W$	$\mathcal{C}(c_2)$	$2 2W$	$6 W$	$1 ^{3W/2}$	$\mathcal{A}(c_2)$	$1 ^{3W/2}$
c_3	$4 ^{W/2}$	$3 2W$	$\mathcal{C}(c_3)$	$2 2W$	$6 W$	$1 ^{3W/2}$	$\mathcal{A}(c_3)$	$1 ^{3W/2}$
c_4	def							
c_5	def							
c_6	def							

h_b

c_1	def								
c_2	def								
c_3	def								
c_4	$5 W$	$1 ^{3W/2}$	$\mathcal{C}(c_4)$	$2 W$	$4 W$	$3 ^{3W/2}$	$1 ^{3W/2}$	$\mathcal{A}(c_4)$	$1 W$
c_5	$5 W$	$1 ^{3W/2}$	$\mathcal{C}(c_5)$	$2 W$	$4 W$	$3 ^{3W/2}$	$1 ^{3W/2}$	$\mathcal{A}(c_5)$	$1 W$
c_6	$5 W$	$1 ^{3W/2}$	$\mathcal{C}(c_6)$	$2 W$	$4 W$	$3 ^{3W/2}$	$1 ^{3W/2}$	$\mathcal{A}(c_6)$	$1 W$