

IASD M2 at Paris Dauphine

# Deep Reinforcement Learning

## 21: Inverse Reinforcement Learning

Eric Benhamou David Sautiel



# Acknowledgement

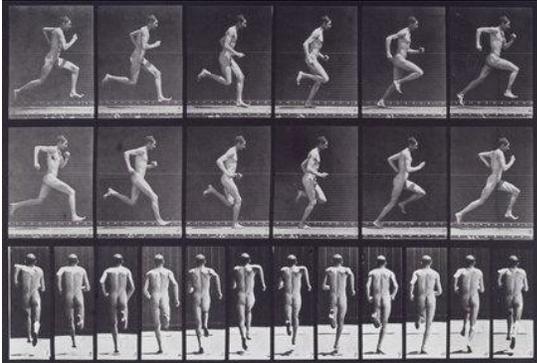
These materials are based on the seminal course of Sergey Levine CS285



# Today's Lecture

1. So far: manually design reward function to define a task
  2. What if we want to *learn* the reward function from observing an expert, and then use reinforcement learning?
  3. Apply approximate optimality model from last time, but now learn the reward!
- Goals:
    - Understand the inverse reinforcement learning problem definition
    - Understand how probabilistic models of behavior can be used to derive inverse reinforcement learning algorithms
    - Understand a few practical inverse reinforcement learning algorithms we can use

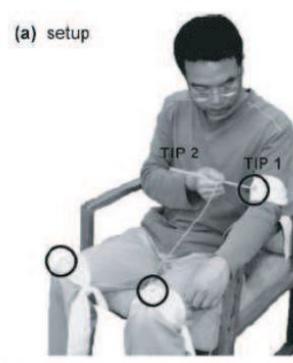
# Optimal Control as a Model of Human Behavior



Muybridge (c. 1870)



Mombaur et al. '09



Li & Todorov '06



Ziebart '08

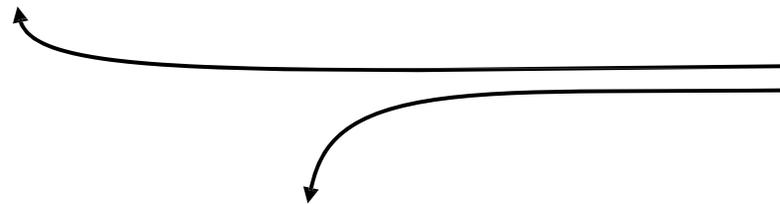
$$\mathbf{a}_1, \dots, \mathbf{a}_T = \arg \max_{\mathbf{a}_1, \dots, \mathbf{a}_T} \sum_{t=1}^T r(\mathbf{s}_t, \mathbf{a}_t)$$

$$\mathbf{s}_{t+1} = f(\mathbf{s}_t, \mathbf{a}_t)$$

$$\pi = \arg \max_{\pi} E_{\mathbf{s}_{t+1} \sim p(\mathbf{s}_{t+1} | \mathbf{s}_t, \mathbf{a}_t), \mathbf{a}_t \sim \pi(\mathbf{a}_t | \mathbf{s}_t)} [r(\mathbf{s}_t, \mathbf{a}_t)]$$

$$\mathbf{a}_t \sim \pi(\mathbf{a}_t | \mathbf{s}_t)$$

optimize this to explain the data

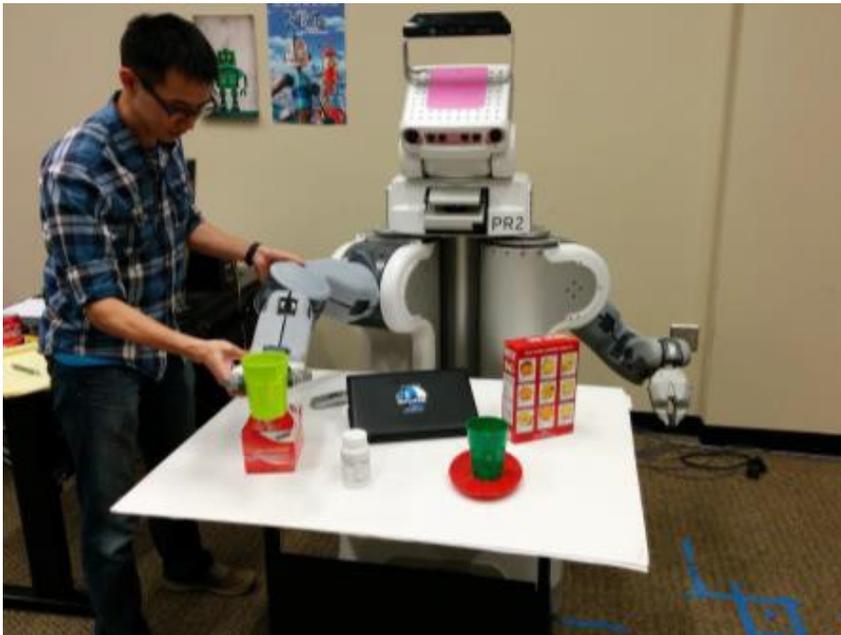


# Why should we worry about learning rewards?

## The imitation learning perspective

### Standard imitation learning:

- copy the *actions* performed by the expert
- no reasoning about outcomes of actions



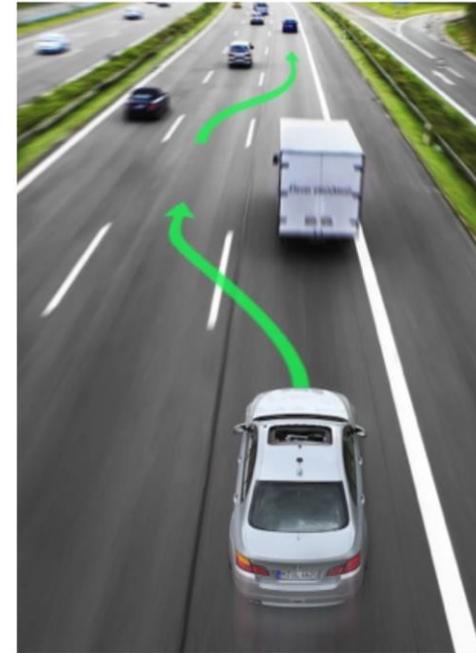
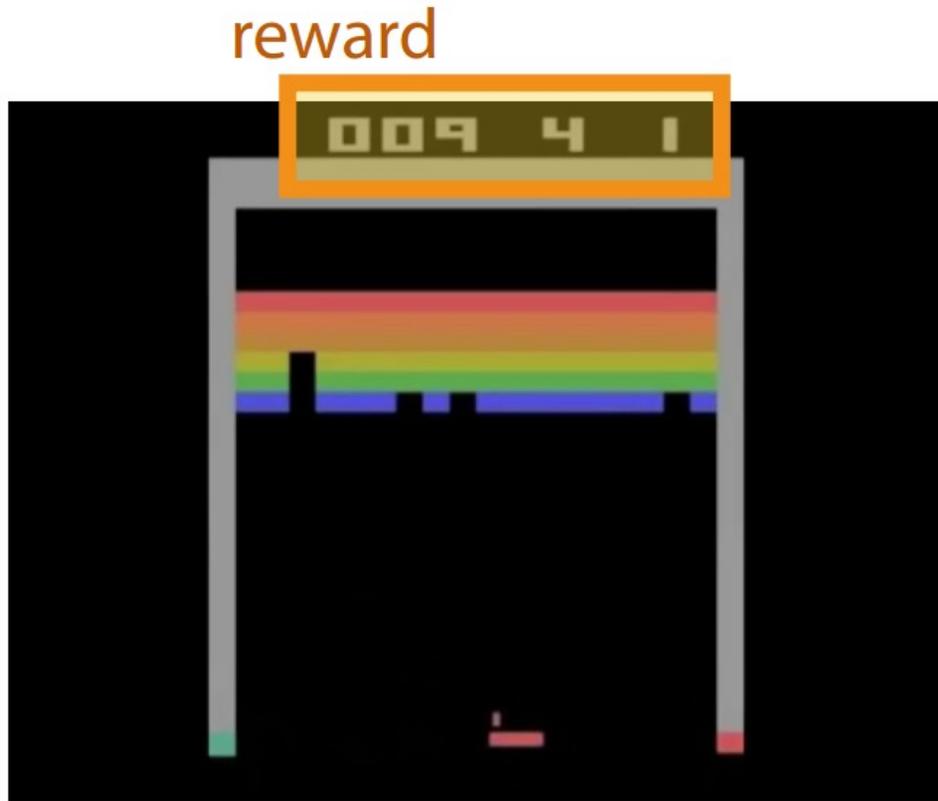
### Human imitation learning:

- copy the *intent* of the expert
- might take very different actions!



# Why should we worry about learning rewards?

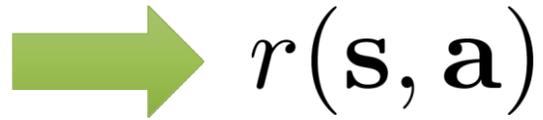
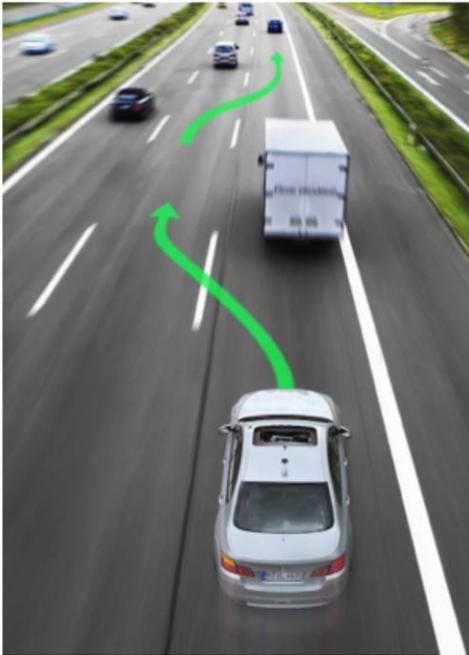
The reinforcement learning perspective



**what is the reward?**

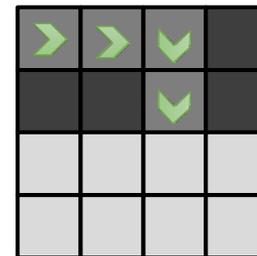
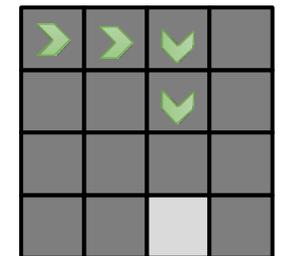
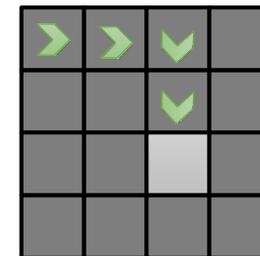
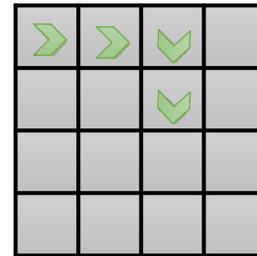
# Inverse reinforcement learning

Infer reward functions from demonstrations



by itself, this is an **underspecified** problem

many reward functions can explain the **same** behavior



# A bit more formally

“forward” reinforcement learning

given:

states  $\mathbf{s} \in \mathcal{S}$ , actions  $\mathbf{a} \in \mathcal{A}$

(sometimes) transitions  $p(\mathbf{s}'|\mathbf{s}, \mathbf{a})$

reward function  $r(\mathbf{s}, \mathbf{a})$

learn  $\pi^*(\mathbf{a}|\mathbf{s})$

inverse reinforcement learning

given:

states  $\mathbf{s} \in \mathcal{S}$ , actions  $\mathbf{a} \in \mathcal{A}$

(sometimes) transitions  $p(\mathbf{s}'|\mathbf{s}, \mathbf{a})$

samples  $\{\tau_i\}$  sampled from  $\pi^*(\tau)$

learn  $r_\psi(\mathbf{s}, \mathbf{a})$

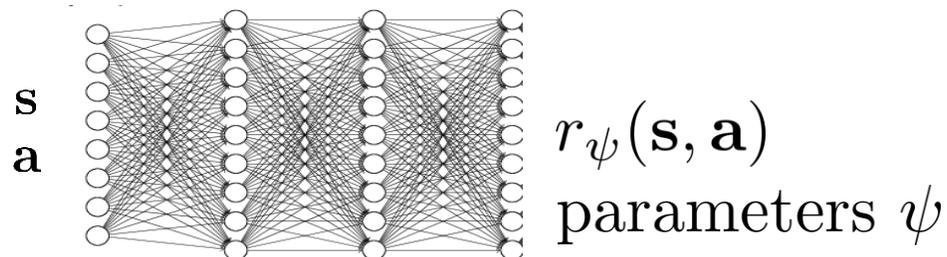
reward parameters

...and then use it to learn  $\pi^*(\mathbf{a}|\mathbf{s})$

neural net reward function:

linear reward function:

$$r_\psi(\mathbf{s}, \mathbf{a}) = \sum_i \psi_i f_i(\mathbf{s}, \mathbf{a}) = \psi^T \mathbf{f}(\mathbf{s}, \mathbf{a})$$



# Feature matching IRL

linear reward function:

$$r_\psi(\mathbf{s}, \mathbf{a}) = \sum_i \psi_i f_i(\mathbf{s}, \mathbf{a}) = \psi^T \mathbf{f}(\mathbf{s}, \mathbf{a})$$

if features  $\mathbf{f}$  are important, what if we match their expectations?

let  $\pi^{r_\psi}$  be the optimal policy for  $r_\psi$

$$\text{pick } \psi \text{ such that } E_{\pi^{r_\psi}}[\mathbf{f}(\mathbf{s}, \mathbf{a})] = E_{\pi^*}[\mathbf{f}(\mathbf{s}, \mathbf{a})]$$

still ambiguous!

state-action marginal under  $\pi^{r_\psi}$

unknown optimal policy  
approximate using expert samples

maximum margin principle:

$$\max_{\psi, m} m \quad \text{such that } \psi^T E_{\pi^*}[\mathbf{f}(\mathbf{s}, \mathbf{a})] \geq \underbrace{\max_{\pi \in \Pi} \psi^T E_\pi[\mathbf{f}(\mathbf{s}, \mathbf{a})]} + m$$

need to somehow “weight” by similarity between  $\pi^*$  and  $\pi$

# Feature matching IRL & maximum margin

remember the “SVM trick”:

$$\max_{\psi, m} m \quad \text{such that } \psi^T E_{\pi^*}[\mathbf{f}(\mathbf{s}, \mathbf{a})] \geq \max_{\pi \in \Pi} \psi^T E_{\pi}[\mathbf{f}(\mathbf{s}, \mathbf{a})] + m$$



$$\min_{\psi} \frac{1}{2} \|\psi\|^2 \quad \text{such that } \psi^T E_{\pi^*}[\mathbf{f}(\mathbf{s}, \mathbf{a})] \geq \max_{\pi \in \Pi} \psi^T E_{\pi}[\mathbf{f}(\mathbf{s}, \mathbf{a})] + D(\pi, \pi^*)$$

e.g., difference in feature expectations!

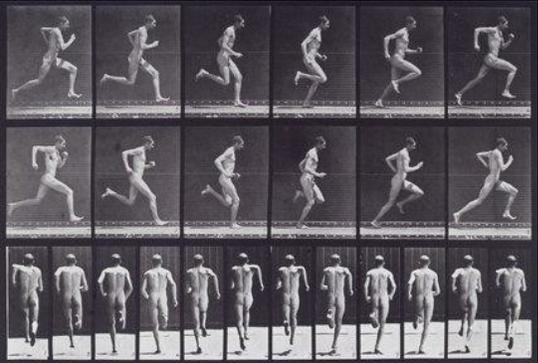
Issues:

- Maximizing the margin is a bit arbitrary
- No clear model of expert suboptimality (can add slack variables...)
- Messy constrained optimization problem – not great for deep learning!

Further reading:

- Abbeel & Ng: Apprenticeship learning via inverse reinforcement learning
- Ratliff et al: Maximum margin planning

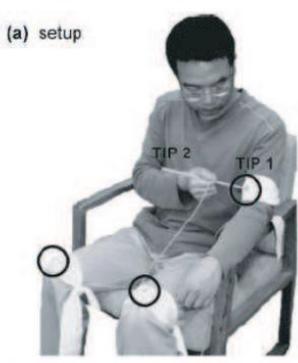
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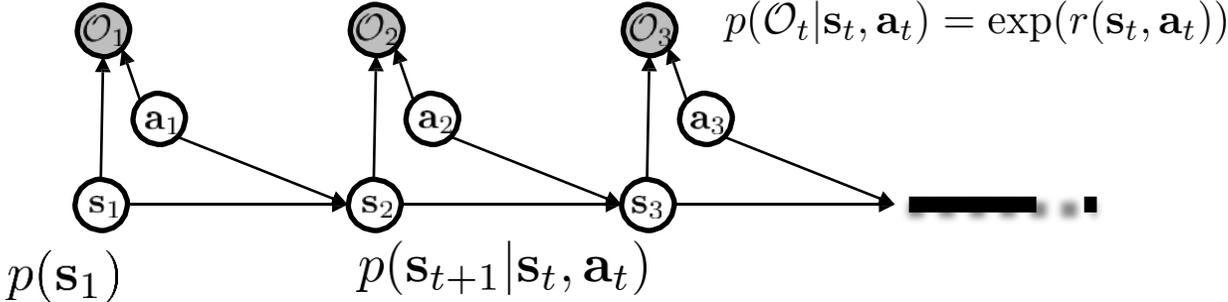


Li & Todorov '06



Ziebart '08

$$p(\mathbf{s}_{1:T}, \mathbf{a}_{1:T} | \mathcal{O}_{1:T})$$



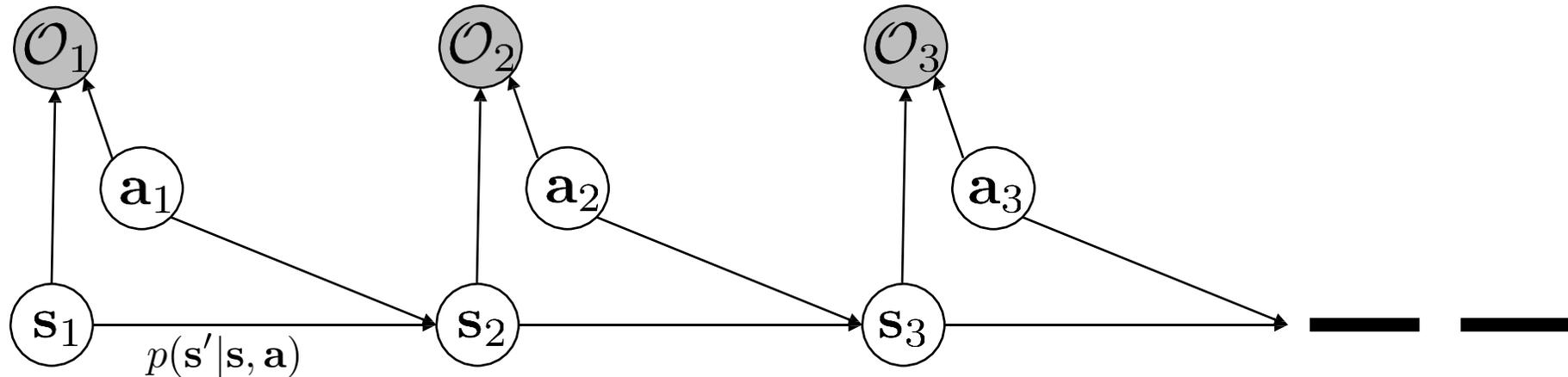
# A probabilistic graphical model of decision making

$$p(\underbrace{\mathbf{s}_{1:T}, \mathbf{a}_{1:T}}_{\tau}) = ?? \quad \text{no assumption of optimal behavior!}$$

$$p(\tau | \mathcal{O}_{1:T}) \quad p(\mathcal{O}_t | \mathbf{s}_t, \mathbf{a}_t) = \exp(r(\mathbf{s}_t, \mathbf{a}_t))$$

$$p(\tau | \mathcal{O}_{1:T}) = \frac{p(\tau, \mathcal{O}_{1:T})}{p(\mathcal{O}_{1:T})}$$

$$\propto p(\tau) \prod_t \exp(r(\mathbf{s}_t, \mathbf{a}_t)) = p(\tau) \exp\left(\sum_t r(\mathbf{s}_t, \mathbf{a}_t)\right)$$



# Learning the Reward Function

# Learning the optimality variable

$$p(\mathcal{O}_t | \mathbf{s}_t, \mathbf{a}_t, \psi) \propto \exp(r_\psi(\mathbf{s}_t, \mathbf{a}_t))$$

reward parameters

given:

samples  $\{\tau_i\}$  sampled from  $\pi^*(\tau)$

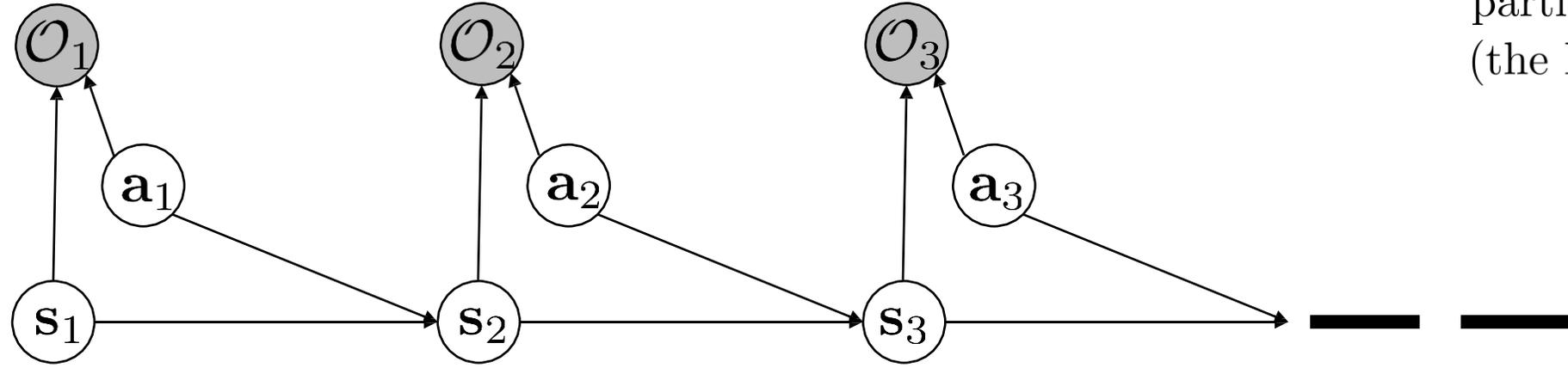
$$p(\tau | \mathcal{O}_{1:T}, \psi) \propto \cancel{p(\tau)} \exp\left(\sum_t r_\psi(\mathbf{s}_t, \mathbf{a}_t)\right)$$

can ignore (independent of  $\psi$ )

maximum likelihood learning:

$$\max_{\psi} \frac{1}{N} \sum_{i=1}^N \log p(\tau_i | \mathcal{O}_{1:T}, \psi) = \max_{\psi} \frac{1}{N} \sum_{i=1}^N r_\psi(\tau_i) - \log Z$$

partition function  
(the hard part)



# The IRL partition function

$$\max_{\psi} \frac{1}{N} \sum_{i=1}^N r_{\psi}(\tau_i) - \log Z \quad Z = \int p(\tau) \exp(r_{\psi}(\tau)) d\tau$$

$$\nabla_{\psi} \mathcal{L} = \frac{1}{N} \sum_{i=1}^N \nabla_{\psi} r_{\psi}(\tau_i) - \underbrace{\frac{1}{Z} \int p(\tau) \exp(r_{\psi}(\tau)) \nabla_{\psi} r_{\psi}(\tau) d\tau}_{p(\tau | \mathcal{O}_{1:T}, \psi)}$$

$$\nabla_{\psi} \mathcal{L} = E_{\tau \sim \pi^*(\tau)} [\nabla_{\psi} r_{\psi}(\tau_i)] - E_{\tau \sim p(\tau | \mathcal{O}_{1:T}, \psi)} [\nabla_{\psi} r_{\psi}(\tau)]$$

 estimate with expert samples

 soft optimal policy under current reward

# Estimating the expectation

$$\begin{aligned} \nabla_{\psi} \mathcal{L} &= E_{\tau \sim \pi^*(\tau)} [\nabla_{\psi} r_{\psi}(\tau)] - \underbrace{E_{\tau \sim p(\tau | \mathcal{O}_{1:T}, \psi)} [\nabla_{\psi} r_{\psi}(\tau)]}_{E_{\tau \sim p(\tau | \mathcal{O}_{1:T}, \psi)} \left[ \nabla_{\psi} \sum_{t=1}^T r_{\psi}(\mathbf{s}_t, \mathbf{a}_t) \right]} \\ &= \sum_{t=1}^T \underbrace{E_{(\mathbf{s}_t, \mathbf{a}_t) \sim p(\mathbf{s}_t, \mathbf{a}_t | \mathcal{O}_{1:T}, \psi)} [\nabla_{\psi} r_{\psi}(\mathbf{s}_t, \mathbf{a}_t)]}_{p(\mathbf{a}_t | \mathbf{s}_t, \mathcal{O}_{1:T}, \psi) p(\mathbf{s}_t | \mathcal{O}_{1:T}, \psi)} \end{aligned}$$

where have we seen this before?

$$= \frac{\beta(\mathbf{s}_t, \mathbf{a}_t)}{\beta(\mathbf{s}_t)} \propto \alpha(\mathbf{s}_t) \beta(\mathbf{s}_t)$$

$$p(\mathbf{a}_t | \mathbf{s}_t, \mathcal{O}_{1:T}, \psi) p(\mathbf{s}_t | \mathcal{O}_{1:T}, \psi) \propto \beta(\mathbf{s}_t, \mathbf{a}_t) \alpha(\mathbf{s}_t)$$

backward message

forward message

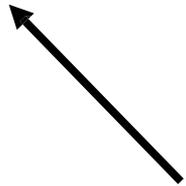
# Estimating the expectation

$$\nabla_{\psi} \mathcal{L} = E_{\tau \sim \pi^*(\tau)} [\nabla_{\psi} r_{\psi}(\tau)] - \underbrace{E_{\tau \sim p(\tau | \mathcal{O}_{1:T}, \psi)} [\nabla_{\psi} r_{\psi}(\tau)]}$$

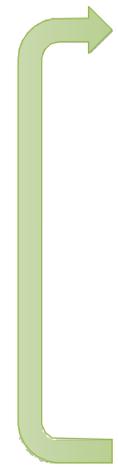
$$\text{let } \mu_t(\mathbf{s}_t, \mathbf{a}_t) \propto \beta(\mathbf{s}_t, \mathbf{a}_t) \alpha(\mathbf{s}_t)$$

$$\begin{aligned} & \sum_{t=1}^T \int \int \mu_t(\mathbf{s}_t, \mathbf{a}_t) \nabla_{\psi} r_{\psi}(\mathbf{s}_t, \mathbf{a}_t) d\mathbf{s}_t d\mathbf{a}_t \\ &= \sum_{t=1}^T \vec{\mu}_t^T \nabla_{\psi} \vec{r}_{\psi} \end{aligned}$$

state-action visitation probability for each  $(\mathbf{s}_t, \mathbf{a}_t)$



# The MaxEnt IRL algorithm



1. Given  $\psi$ , compute backward message  $\beta(\mathbf{s}_t, \mathbf{a}_t)$  (see previous lecture)
2. Given  $\psi$ , compute forward message  $\alpha(\mathbf{s}_t)$  (see previous lecture)
3. Compute  $\mu_t(\mathbf{s}_t, \mathbf{a}_t) \propto \beta(\mathbf{s}_t, \mathbf{a}_t)\alpha(\mathbf{s}_t)$
4. Evaluate  $\nabla_{\psi} \mathcal{L} = \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\psi} r_{\psi}(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) - \sum_{t=1}^T \int \int \mu_t(\mathbf{s}_t, \mathbf{a}_t) \nabla_{\psi} r_{\psi}(\mathbf{s}_t, \mathbf{a}_t) d\mathbf{s}_t d\mathbf{a}_t$
5.  $\psi \leftarrow \psi + \eta \nabla_{\psi} \mathcal{L}$

## Why MaxEnt?

in the case where  $r_{\psi}(\mathbf{s}_t, \mathbf{a}_t) = \psi^T \mathbf{f}(\mathbf{s}_t, \mathbf{a}_t)$ , we can show that it optimizes

$$\max_{\psi} \mathcal{H}(\pi^{r_{\psi}}) \text{ such that } E_{\pi^{r_{\psi}}}[\mathbf{f}] = E_{\pi^*}[\mathbf{f}]$$

optimal max-ent policy under  $r^{\psi}$

unknown expert policy  
estimated with samples

as random as possible  
while matching features

# Maximum Entropy Inverse Reinforcement Learning

Brian D. Ziebart, Andrew Maas, J. Andrew Bagnell, and Anind K. Dey

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# Approximations in High Dimensions

# What's missing so far?

- MaxEnt IRL so far requires...
  - Solving for (soft) optimal policy in the inner loop
  - Enumerating all state-action tuples for visitation frequency and gradient
- To apply this in practical problem settings, we need to handle...
  - Large and continuous state and action spaces
  - States obtained via sampling only
  - Unknown dynamics

# Unknown dynamics & large state/action spaces

Assume we don't know the dynamics, but we can sample, like in standard RL

recall:

$$\nabla_{\psi} \mathcal{L} = E_{\tau \sim \pi^*(\tau)} [\nabla_{\psi} r_{\psi}(\tau_i)] - E_{\tau \sim p(\tau | \mathcal{O}_{1:T}, \psi)} [\nabla_{\psi} r_{\psi}(\tau)]$$

estimate with expert samples

soft optimal policy under current reward

idea: learn  $p(\mathbf{a}_t | \mathbf{s}_t, \mathcal{O}_{1:T}, \psi)$  using any max-ent RL algorithm

then run this policy to sample  $\{\tau_j\}$

$$J(\theta) = \sum_t E_{\pi(\mathbf{s}_t, \mathbf{a}_t)} [r_{\psi}(\mathbf{s}_t, \mathbf{a}_t)] + E_{\pi(\mathbf{s}_t)} [\mathcal{H}(\pi(\mathbf{a} | \mathbf{s}_t))]$$

$$\nabla_{\psi} \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\psi} r_{\psi}(\tau_i) - \frac{1}{M} \sum_{j=1}^M \nabla_{\psi} r_{\psi}(\tau_j)$$

sum over expert samples

sum over policy samples

# More efficient sample-based updates

$$\nabla_{\psi} \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\psi} r_{\psi}(\tau_i) - \frac{1}{M} \sum_{j=1}^M \nabla_{\psi} r_{\psi}(\tau_j)$$

sum over expert samples

sum over policy samples

improve ~~learn~~  $p(\mathbf{a}_t | \mathbf{s}_t, \mathcal{O}_{1:T}, \psi)$  using any max-ent RL algorithm  
(a little)  
then run this policy to sample  $\{\tau_j\}$

looks expensive! what if we use “lazy” policy optimization?

problem: estimator is now biased! wrong distribution!

solution 1: use importance sampling

$$\nabla_{\psi} \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\psi} r_{\psi}(\tau_i) - \frac{1}{\sum_j w_j} \sum_{j=1}^M w_j \nabla_{\psi} r_{\psi}(\tau_j) \quad w_j = \frac{p(\tau) \exp(r_{\psi}(\tau_j))}{\pi(\tau_j)}$$

# Importance sampling

$$\nabla_{\psi} \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\psi} r_{\psi}(\tau_i) - \frac{1}{\sum_j w_j} \sum_{j=1}^M w_j \nabla_{\psi} r_{\psi}(\tau_j)$$

$$w_j = \frac{p(\tau) \exp(r_{\psi}(\tau_j))}{\pi(\tau_j)}$$

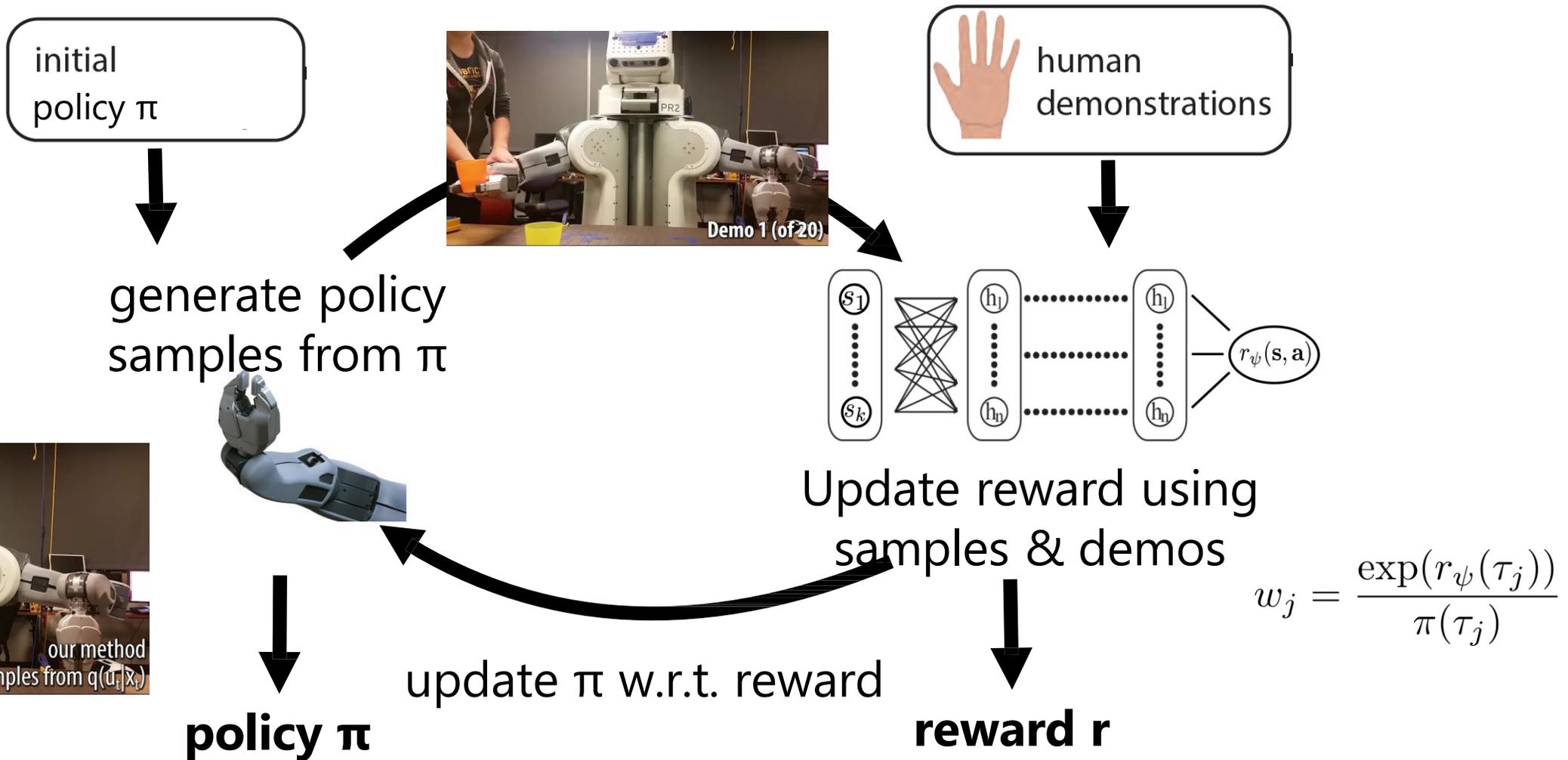


$$\begin{aligned} & \frac{\cancel{p(\mathbf{s}_1)} \prod_t \cancel{p(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)} \exp(r_{\psi}(\mathbf{s}_t, \mathbf{a}_t))}{\cancel{p(\mathbf{s}_1)} \prod_t \cancel{p(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)} \pi(\mathbf{a}_t|\mathbf{s}_t)} \\ &= \frac{\exp(\sum_t r_{\psi}(\mathbf{s}_t, \mathbf{a}_t))}{\prod_t \pi(\mathbf{a}_t|\mathbf{s}_t)} \end{aligned}$$

each policy update w.r.t.  $r_{\psi}$  brings us closer to the target distribution!

# guided cost learning algorithm

(Finn et al. ICML '16)



$$\nabla_\psi \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_\psi r_\psi(\tau_i) - \frac{1}{\sum_j w_j} \sum_{j=1}^M w_j \nabla_\psi r_\psi(\tau_j)$$

# IRL and GANs

# It looks a bit like a game...

initial  
policy  $\pi$



samples from  $\pi_\theta(\tau)$

$$\nabla_\theta \mathcal{L} \approx \frac{1}{M} \sum_{j=1}^M \nabla_\theta \log \pi_\theta(\tau_j) r_\psi(\tau_j)$$

policy changed to make it *harder* to distinguish from demos

 human  
demonstrations



samples from  $\pi^*(\tau)$



$$\nabla_\psi \mathcal{L} \approx \frac{1}{N} \sum_{i=1}^N \nabla_\psi r_\psi(\tau_i) - \frac{1}{\sum_j w_j} \sum_{j=1}^M w_j \nabla_\psi r_\psi(\tau_j)$$

demos are made more likely, samples less likely

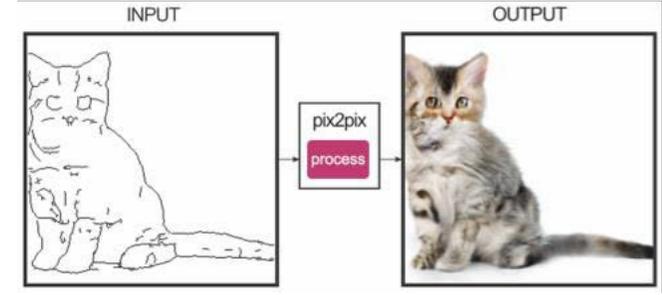
# Generative Adversarial Networks



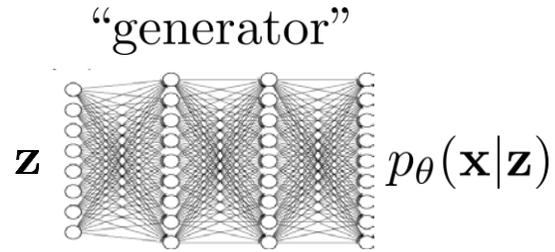
Zhu et al. '17



Arjovsky et al. '17



Isola et al. '17



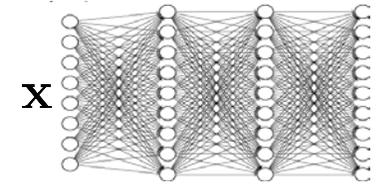
samples from  $p_\theta(\mathbf{x})$

data (“demonstrations”)



samples from  $\pi_\theta(\tau)$

$$D(\mathbf{x}) = p_\psi(\text{real image}|\mathbf{x})$$

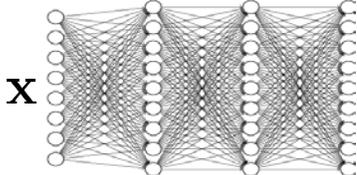


$$\psi = \arg \max_{\psi} \frac{1}{N} \sum_{\mathbf{x} \sim p^*} \log D_\psi(\mathbf{x}) + \frac{1}{M} \sum_{\mathbf{x} \sim p_\theta} \log(1 - D_\psi(\mathbf{x}))$$

$$\theta \leftarrow \arg \max_{\theta} E_{\mathbf{x} \sim p_\theta} \log D_\psi(\mathbf{x})$$

# Inverse RL as a GAN

$$D(\mathbf{x}) = p_\psi(\text{real image}|\mathbf{x})$$



which discriminator is best?

$$D^*(\mathbf{x}) = \frac{p^*(\mathbf{x})}{p_\theta(\mathbf{x}) + p^*(\mathbf{x})}$$

for IRL, optimal policy approaches  $\pi_\theta(\tau) \propto p(\tau) \exp(r_\psi(\tau))$

choose this parameterization for discriminator:

optimize  $Z$  w.r.t. same objective as  $\psi$ !

$$D_\psi(\tau) = \frac{p(\tau) \frac{1}{Z} \exp(r(\tau))}{p_\theta(\tau) + p(\tau) \frac{1}{Z} \exp(r(\tau))} = \frac{\cancel{p(\tau)} \frac{1}{Z} \exp(r(\tau))}{\cancel{p(\tau)} \prod_t \pi_\theta(\mathbf{a}_t|\mathbf{s}_t) + \cancel{p(\tau)} \frac{1}{Z} \exp(r(\tau))} = \frac{\frac{1}{Z} \exp(r(\tau))}{\prod_t \pi_\theta(\mathbf{a}_t|\mathbf{s}_t) + \frac{1}{Z} \exp(r(\tau))}$$

optimize this w.r.t.  $\psi$

$$\psi \leftarrow \arg \max_{\psi} E_{\tau \sim p^*} [\log D_\psi(\tau)] + E_{\tau \sim \pi_\theta} [\log(1 - D_\psi(\tau))]$$

we don't need importance weights anymore – they are subsumed into  $Z$

# Inverse RL as a GAN

generator/policy

$\pi_\theta(\tau)$



samples from  $\pi_\theta(\tau)$

data/demonstrations



samples from  $p^*(\tau)$



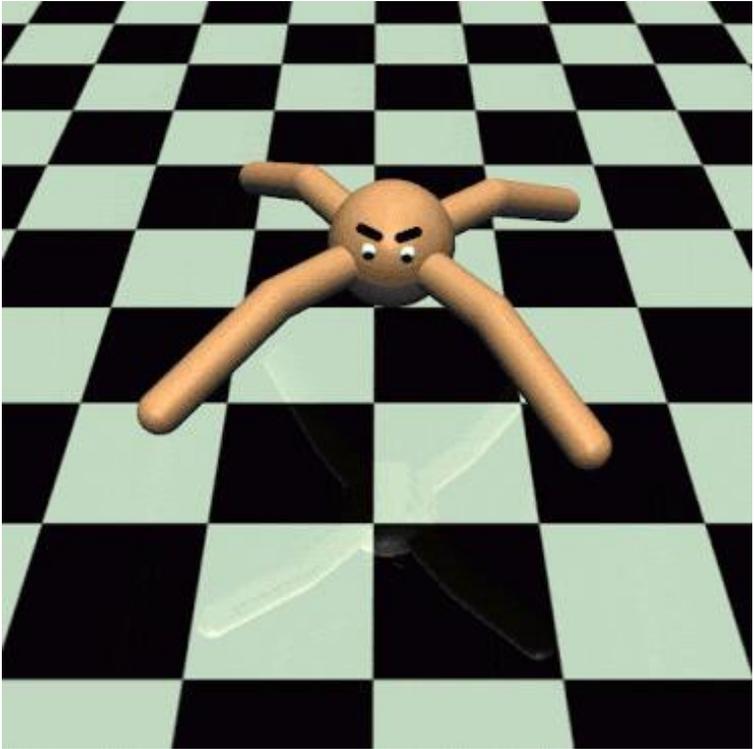
$$\psi \leftarrow \arg \max_{\psi} E_{\tau \sim p^*} [\log D_{\psi}(\tau)] + E_{\tau \sim \pi_{\theta}} [\log(1 - D_{\psi}(\tau))]$$

$$\nabla_{\theta} \mathcal{L} \approx \frac{1}{M} \sum_{j=1}^M \nabla_{\theta} \log \pi_{\theta}(\tau_j) r_{\psi}(\tau_j)$$

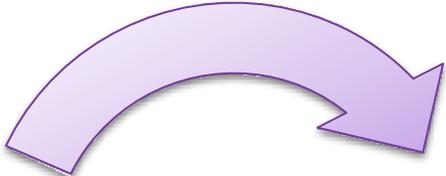
$$D_{\psi}(\tau) = \frac{\frac{1}{Z} \exp(r(\tau))}{\prod_t \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t) + \frac{1}{Z} \exp(r(\tau))}$$

policy changed to make it *harder* to distinguish from demos

# Generalization via inverse RL



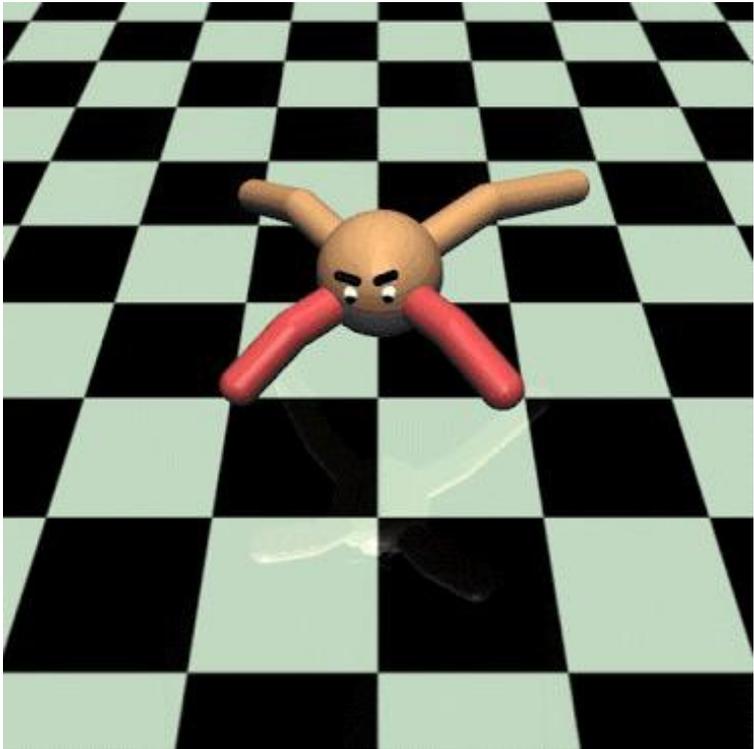
demonstration



what can we learn from the demonstration to enable better transfer?

need to decouple the goal from the dynamics!

policy = reward + dynamics



reproduce behavior under different conditions

# Can we just use a regular discriminator?

generator/policy

$\pi_{\theta}(\tau)$



samples from  $\pi_{\theta}(\tau)$

data/demonstrations



samples from  $p^*(\tau)$



$$\psi \leftarrow \arg \max_{\psi} E_{\tau \sim p^*} [\log D_{\psi}(\tau)] + E_{\tau \sim \pi_{\theta}} [\log(1 - D_{\psi}(\tau))]$$

$$\nabla_{\theta} \mathcal{L} \approx \frac{1}{M} \sum_{j=1}^M \nabla_{\theta} \log \pi_{\theta}(\tau_j) \log D_{\psi}(\tau_j)$$

$D_{\psi}(\tau)$  = standard binary neural net classifier

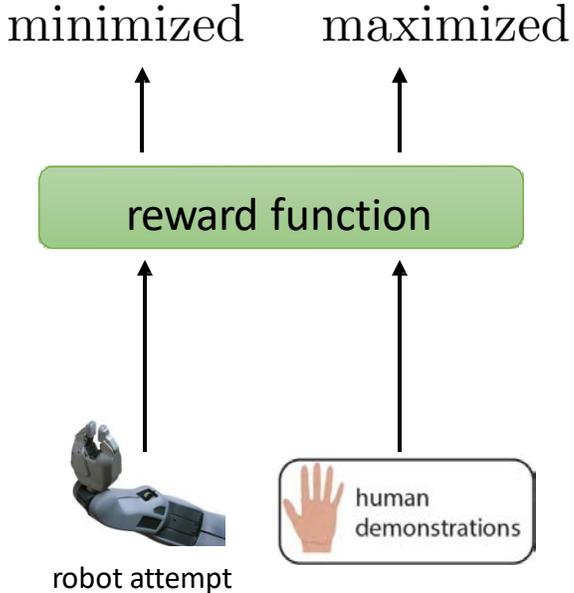
policy changed to make it *harder* to distinguish from demos

## Pros & cons:

- + often simpler to set up optimization, fewer moving parts
- discriminator knows *nothing* at convergence
- generally cannot reoptimize the "reward"

# IRL as adversarial optimization

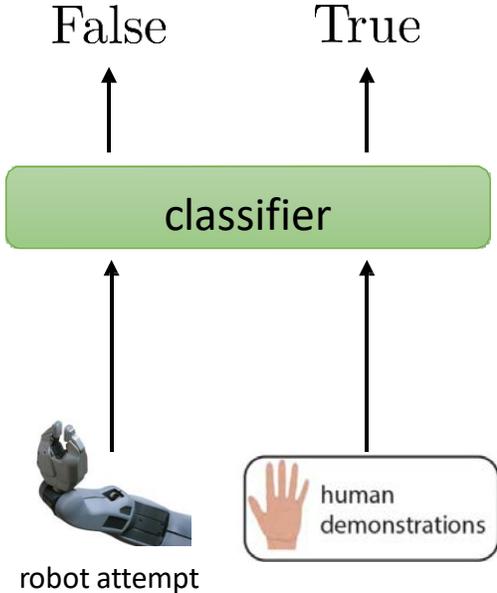
Guided Cost Learning  
 Finn et al., ICML 2016



learns distribution  $p(\tau)$  such that demos have max likelihood  
 $p(\tau) \propto \exp(r(\tau))$  (MaxEnt model)

$$D(\tau) = \frac{\frac{1}{Z} \exp(r(\tau))}{\frac{1}{Z} \exp(r(\tau)) + \pi(\tau)}$$

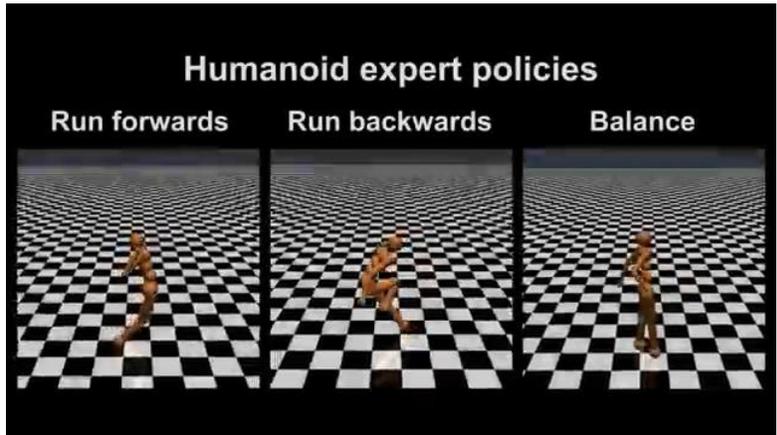
Generative Adversarial Imitation Learning  
 Ho & Ermon, NIPS 2016



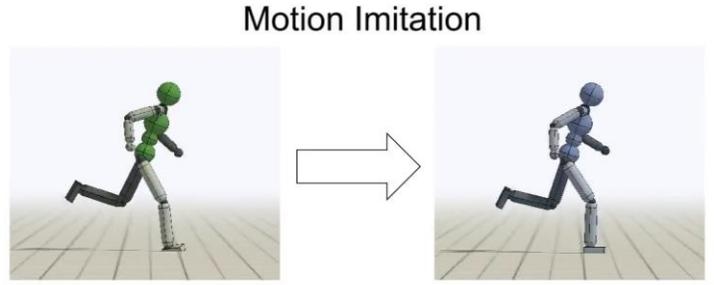
$D(\tau)$  = probability  $\tau$  is a demo  
 use  $\log D(\tau)$  as “reward”

$$D(\tau) = \text{some classifier}$$

actually the same thing!



Hausman, Chebotar, Schaal, Sukhatme, Lim



the goal is to train a simulated character to imitate the motion.

Peng, Kanazawa, Toyer, Abbeel, Levine

# Suggested Reading on Inverse RL

## **Classic Papers:**

Abbeel & Ng ICML '04. *Apprenticeship Learning via Inverse Reinforcement Learning*.

Good introduction to inverse reinforcement learning

Ziebart et al. AAAI '08. *Maximum Entropy Inverse Reinforcement Learning*. Introduction to probabilistic method for inverse reinforcement learning

## **Modern Papers:**

Finn et al. ICML '16. *Guided Cost Learning*. Sampling based method for MaxEnt IRL that handles unknown dynamics and deep reward functions

Wulfmeier et al. arXiv '16. *Deep Maximum Entropy Inverse Reinforcement Learning*.

MaxEnt inverse RL using deep reward functions

Ho & Ermon NIPS '16. *Generative Adversarial Imitation Learning*. Inverse RL method using generative adversarial networks

Fu, Luo, Levine ICLR '18. Learning Robust Rewards with Adversarial Inverse Reinforcement Learning