## IA Solutions 3: Constraint Satisfaction

## Exercise 1

The algorithm effectively performs a depth first search, backtracking when the constraints are violated.


## Exercise 2

We write $D(n)$ for the possible values for a variable $n$. Arc consistency from $n$ to $n^{\prime}$ is satisfied if $\forall v \in D(n), \exists v^{\prime} \in D\left(n^{\prime}\right)$ such that $n=v$ and $n^{\prime}=v^{\prime}$ is consistent. If there is no such $v^{\prime}$, we remove $v$ from $D(n)$. If after doing this $D(n)$ is empty, the search down this branch has failed.


## Exercise 3

If we apply all the heuristics at once, this finds the solution directly: F, S and I have minimal sets of possible variables, and out of these F can constrain the most other variables. We assign green to F first as this only constrains E, whereas blue constains $S$ and I. The next node to assign is either $S$ or $I$, to either blue or red. The final two variables may be assigned any of their remaining colours.

